

The hypotheses represent all possible states in the system. Pieces of evidence are symptoms or events that occur or may occur in the system. Data sources are persons or organizations that provide information for a scenario. There are several terms used in DST: basic assignment (m), belief (bel), and plausibility (pl).

$$bel A = \sum_{B \subseteq A; B \neq \emptyset} m(B) \tag{1}$$

$$pl A = \sum_{B \cap A \neq \emptyset} m(B) \tag{2}$$

$$m_{1,2} Z = \frac{A \cap B = Z \neq \emptyset m_1 A m_2(B)}{1 - \sum_{A \cap B = Z \neq \emptyset} m_1 A m_2(B)} \tag{3}$$

Fuzzy Logic

Fuzzy logic is developed from the theory of fuzzy set by Lotfi Zadeh (1965). Fuzzy logic has been extended to handle the concept of partial truth, where the truth value may range between completely true and completely false. Fuzzy set used words and not number to represent certain condition like “no”, “few”, “some”, “many”, “yes”. Membership function in fuzzy logic represent the degree of truth in the real world and this will need a good formulation. There are a few type of fuzzy logic membership function, but triangular and trapezoidal is the most commonly used.

Triangular membership function formed by three parameters (a, b, c) which ($a < b < c$).

$$Triangle\ x; a, b, c = \begin{cases} 0, & x \leq a \\ \frac{x-a}{b-a} & a \leq x \leq b \\ \frac{c-x}{c-b} & b \leq x \leq c \\ 0, & c \leq x \end{cases} \tag{4}$$

Trapezoidal membership function formed by four parameters (a, b, c, d) which ($a < b < c < d$).

$$Trapezoidal\ x; a, b, c, d = \begin{cases} 0, & x \leq a \\ \frac{x-a}{b-a} & a \leq x \leq b \\ 1, & b \leq x \leq c \\ \frac{d-x}{d-c} & c \leq x \leq d \\ 0, & d \leq x \end{cases} \tag{5}$$

Fuzzy Logic Process

Fuzzy logic has three steps in the process: fuzzification, rule evaluation, and defuzzification. Fuzzification is a process to transform crisp values into grades of membership for linguistic terms of fuzzy set. The membership function is used to associate a grade to each linguistic term.

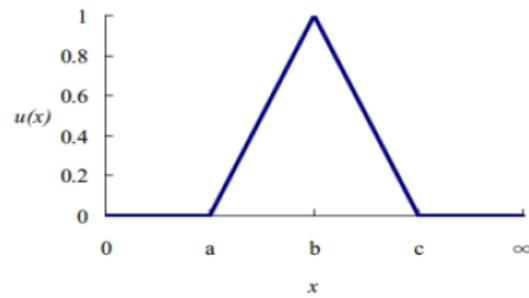


Figure 2. Triangular membership function

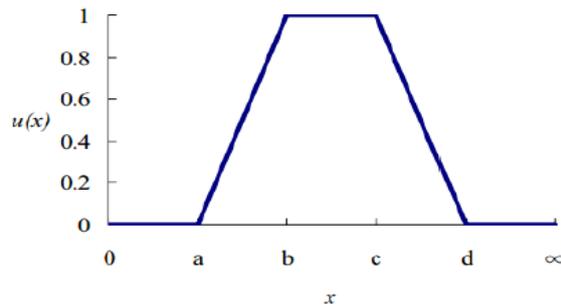


Figure 3. Trapezoidal membership function

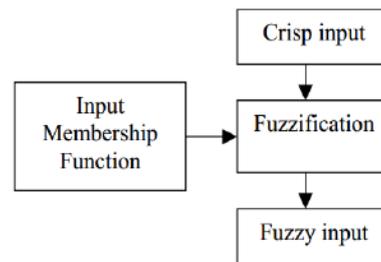


Figure 4. Fuzzification process

Rule evaluation is a process to find fuzzy output from fuzzy input based on if-then rules.

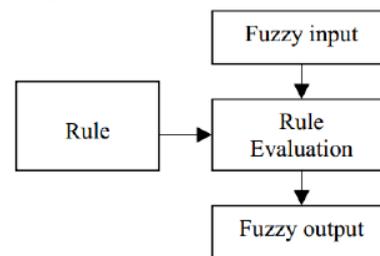


Figure 5. Rule evaluation process

Defuzzification is a process to transform fuzzy output into crisp output using output membership function.

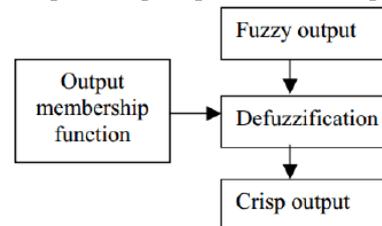


Figure 6. Defuzzification process

Results and Discussion

Failure Identification

Application of fuzzy logic RCM is held in an international thread manufacturing company in Surabaya, Indonesia. There three type of machine used in the process of thread manufacturing: doubling, twisting, and winding machines. Each machine is identified for component failure which caused the production stopped. This company used four type of maintenance: preventive maintenance, corrective maintenance, condition based maintenance, dan breakdown maintenance. RCM decision diagram is build based on maintenance system available in the company.

Decission to use certain type of maintenance for each failure most of the time is based on experience of the maintenance staff in the company. Most of the time there is no absolute “yes” or “no” for every question asked in this RCM decision diagram. Fuzzy logic will be used to solve the problem by giving degree of truth gradually.

Fuzzy inference model requires: fuzzy input output variable, membership function and if_then rules. Fuzzy input variables consist of: failure effect, failure pattern, failure symptom. Input membership function is build by creating linguistic label for each input variable. The label for failure effect started from “very low”, “low”, “medium”, “high” and “very high”. The label for failure patern and failure symptom started from “very clear”, “clear”, “medium”, “not clear” and “very not clear”.

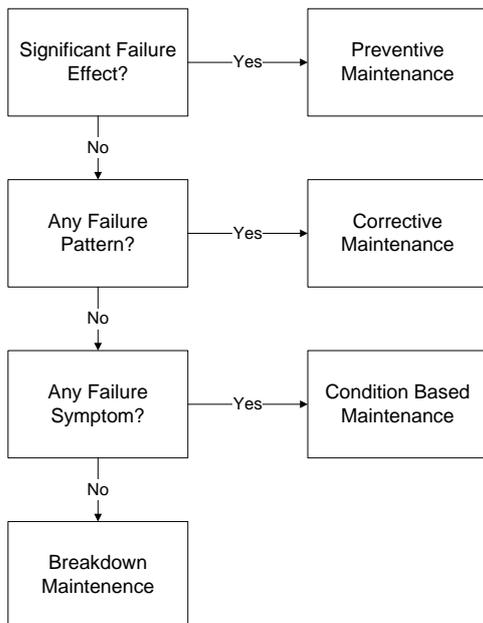


Figure 7. RCM decision diagram

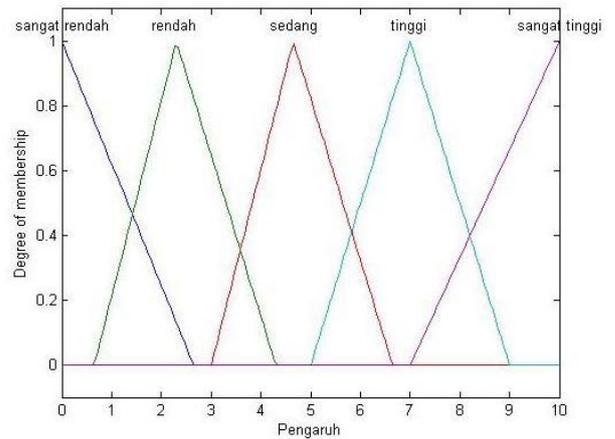


Figure 8. Membership function of failure effect

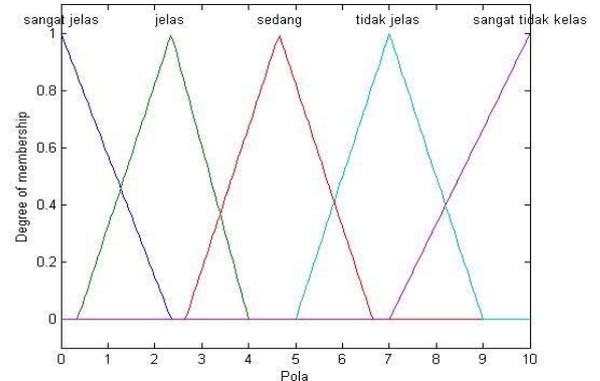


Figure 9. Membership function of failure pattern

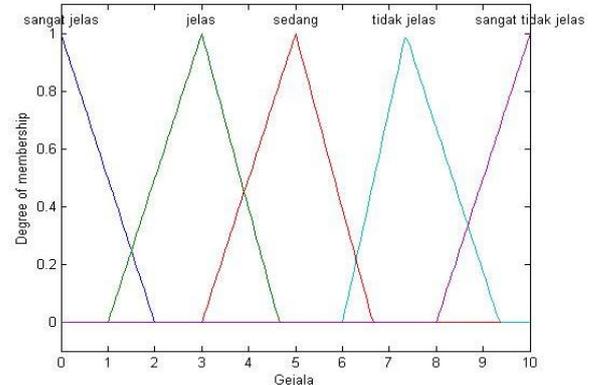


Figure 10. Membership function of failure symptom

There are 72 rules based on combination of the input variables. These rules used to decide type of maintenance based on fuzzy output variables. Since there are four type of maintenance used in the company, output variables also devided evenly to accommodate this.

- Preventive maintenance, between 0 and 2.5.
- Corrective maintenance, between 2.5 and 5.
- Condition Based Maintenance, between 5 and 7.5.
- Breakdown Maintenance, between 7.5 and 10.

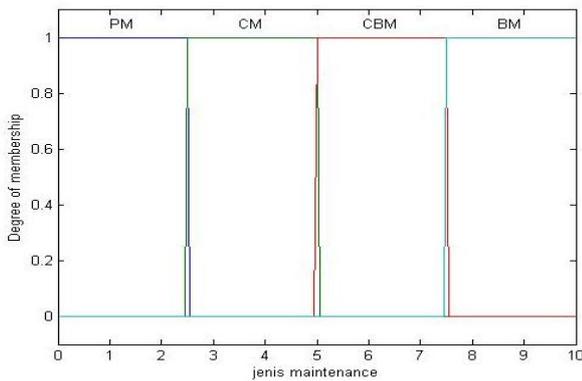


Figure 11. Membership function of maintenance type

The result of fuzzy logic RCM application in this company shows that preventive maintenance should be used for component that has high failure effect, while component with clear failure pattern should use condition based maintenance. Condition based maintenance and breakdown maintenance are suitable for component with clear failure symptom.

Conclusion

Fuzzy Logic RCM can be applied to help company to determined maintenance strategy which fit with current and future condition. Fuzzy logic gives degrees of truth for uncertain answer required by RCM.

References

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Table 1. Result of fuzzy logic RCM

Machine	Component	Effect	Pattern	Symptom	Maintenance
Doubling	Automatic	2,325	4,5	4,675	3,75 CM
	wire				
	Roll	2,325	9,35	5	6,25 CDM
	Gear	3	7,35	2,675	6,25 CDM
	Eyelet	2,325	4,5	4,825	3,75 CM
Twisting	Ear	2,325	4,5	4,825	3,75 CM
	Vanbelt	10	2,35	1,35	1,25 PM
	Wire	4,5	9,35	7,35	8,75 BM
	Yarn Guide	1,35	8,65	7,175	8,75 BM
	Handle	2,675	4,5	4,175	3,75 CM
Winding	Pig tail	2,325	7,35	7,825	8,75 BM
	Tire	4,675	1,65	3,175	3,75 CM
	Tensor socket	2,325	7,35	1,175	6,25 CDM
	Scissor	2	4,5	5	3,75 CM
	Vanbelt	10	2,35	1,35	1,25 PM
	Ceramic	2,325	7,35	7,325	8,75 BM
	Seal	10	2,175	1,325	1,25 PM

PM : Preventive Maintenance
 CM : Corrective Maintenance
 CDM : Condition Based Maintenance
 BM : Breakdown Maintenance

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