ISSN 1411-2485 (Print) ISSN 2087-7439 (Online)

Jurnal **Teknik Industri** Jurnal Keilmuan dan Aplikasi Teknik Industri

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7/15/2015 Vol 16, No 2 (2014)

 Petra Christian University. It available online supported by Directorate General of Higher Education - Ministry of National Education - Republic of Indonesia.

Supported by:

Citation data from Google **Scholar**

Editor and Administration Address:

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The Effect of Unreliable Machine for Two Echelons Deteriorating Inventory Model

I Nyoman Sutapa1, I Gede Agus Widyadana1*

Abstract: Many researchers have developed two echelons supply chain, however only few of them consider deteriorating items and unreliable machine in their models In this paper, we develop an inventory deteriorating model for two echelons supply chain with unreliable machine. The unreliable machine time is assumed uniformly distributed. The model is solved using simple heuristic since a closed form model can not be derived. A numerical example is used to show how the model works. A sensitivity analysis is conducted to show effect of different lost sales cost in the model. The result shows that increasing lost sales cost will increase both manufacture and buyer costs however buyer's total cost increase higher than manufacture's total cost as manufacture's machine is more unreliable.

Keywords: EPQ, deteriorating items, two echelons, unreliable machine.

Introduction

Economic production quantity (EPQ) for deteriorating items models have been developed intensively since the first model was developed by Misra [1]. The first model was very simple and had many assumptions such as constant demand and perfect production process. Later, many researchers try to make the model more realistic by considering unreliable production process. Zequeira *et al.* [2] developed a model to optimize maintenance policy and buffer inventory. They assumed that manufacturing policy is not reliable and need to be maintained. During maintenance period, buffer need to be provided to satisfy demand during the interruption period.

Abboud *et al.* [3] introduced EPQ for deteriorating items model with stochastic machine unavailability. Ideally, machine will start production run when inventory level equal to zero. In some periods, there are possibilities that machine is not ready for some reasons. When inventory level equal to zero and machine is not ready, then shortage will occur. Chung *et al.* [4] extended the work of Abboud [3] by considering deteriorating items. Then Wee and Widyadana [5] considered stochastic time of preventive maintenance and breakdown machine, where machine can breakdowns anytime during production up time.

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Later Wee and Widyadana [6] developed two echelons supply chain by considering unreliable machine; however they did not considering deteriorating items in their model. In this paper, we extend the work of Wee and Widyadana [6] by considering deteriorating items and lost sales. Lost sales occur if the buyer has urgent need and will not wait for next replenishment. The purpose of this study is to determine the optimal production up time to minimize total cost.

This paper is organized as follows. The research motivation and the literature review are presented in Section 1. The mathematical model development are discussed in Section 2. A numerical example are presented in Section 3 and conclusions and future research are given in the last section.

Methods

The assumptions: Production rate is greater than demand rate. No machine breakdown occurs in production run period. Production and demand rate are constant. Deteriorating rate is constant. There is no repair or replacement for a deteriorated item.

Parameters:

- *p* = production rate
- $d =$ demand rate
- $\theta_{\rm v}$ = manufacture deteriorating rate
- θ_{h} = buyer deteriorating rate
- $Cs = setup cost$
- C_t = transportation cost
- $Hv =$ manufacture holding cost
- $Hb =$ buyer holding cost
- *S* = lost sales cost

^{*}Corresponding author

Variables:

- *I* = inventory level
- *T* = replenishment period
- *T¹* = production period
- *T^d* = non production period
- *T^s* = shortage period
- *m* = delivery quantity unit
- $K = \text{frequency of delivery}$

The manufacture inventory model is shown in Figure 1. The manufacture produces products for *wTN/K* time and delivers *m* units every shipment. The manufacture's production unit in one replenishment period is:

$$
Q = wP \frac{T}{K} \tag{1}
$$

For small θ ^{*v*}, the manufacture's total inventory can be modeled as:

$$
I_T = \frac{m^2 K(K - w + 1)}{2d} \tag{2}
$$

The inventory level at the end of production period is equal with inventory level at the beginning of non production period, and one has:

$$
(P - (d + \theta v))\frac{wT}{K} = (d + \theta v)\left(T - \frac{wT}{K}\right)
$$
 (3)

After some simplifications, we have:

$$
w = \frac{(d + \theta v)K}{P}
$$
 (4)

The manufacture's total cost consists of the manufacture's setup cost and holding cost. The manufacture's

total cost can be modeled as follows:
\n
$$
m^{2}K(K - \frac{(d+\theta_{v})K}{p} + 1)H_{v}
$$
\n
$$
TCM(T, K) = \frac{Cs + \frac{Q}{1 - \frac{Q}{2d}}}{T + \int_{t=T_{d}}^{\infty} (t - T_{d})f(t)dt}
$$
\n(5)

The buyer's inventory level is shown in Figure 2. When the inventory level is equal to zero, *m* units of product will be delivered from the manufacture. In this model we assume that delivery lead time is zero. However, there is a possibility that the manufacture delays its shipment resulting in the buyer's lost sales during the period *Ts*. The buyer's inventory cost using the model from Rau *et al.* [6] can be modeled as:

$$
IB = \left(\frac{d(2+\theta_b T)_K}{\theta_b^2 (2-\theta_b T)_K}\right) - \frac{d+d\theta_b T)_K}{\theta_b^2} \left(\frac{H_b K}{T}\right) \tag{6}
$$

The buyer's total inventory cost consists of setup cost.

cost, transportation cost, holding cost, and lost sales cost.
\n
$$
C tK + \left(\frac{d\left(2 + \frac{\theta_s T}{K}\right)}{\theta_s^2 \left(2 - \frac{\theta_s T}{K}\right)} - \frac{d\left(1 + \frac{\theta_s T}{K}\right)}{\theta_s^2}\right) (H_s K) + S_s d \int_{t=T_s}^{\infty} (t - T_a) f(t) dt
$$
\n(7)

Figure 2. The buyer inventory level

The total supply chain cost can be modeled by

combining (5) and (7), one has:
\n
$$
c_3 + \frac{m^2 K (K - \frac{(d+\theta_r)K}{p} + 1)H_r}{2d} + C K + \left(\frac{d \left(2 + \frac{\theta_r T}{K}\right)}{\theta_s^2 \left(2 - \frac{\theta_r T}{K}\right)} - \frac{d \left(1 + \frac{\theta_r T}{K}\right)}{\theta_s^2}\right) H_s K) + S_b D_{i \pi r_s}^{\dagger} (t - T_s) f(t) dt
$$
\n(8)

Uniform Distribution Unavailability Time Model

In this paper, we assume that the unavailability time *t* is a random variable uniformly distributed over the interval [0, b]. The probability density function, $f(t)$, is given as:

$$
f(t) = \begin{cases} 1/b, & 0 \le t \le b \\ 0, & otherwise \end{cases}
$$

Substitute the uniform probability density function modeled as:

in (8), the supply chain total cost per unit time can be modeled as:
\n
$$
c_{s+(d+\theta,\mathcal{T}-mk)}\frac{H_{s}}{\theta_{s}}+C_K+\left(\frac{d\left(2+\frac{\theta_{s}T}{K}\right)}{\theta_{s}^{2}\left(2-\frac{\theta_{s}T}{K}\right)}-\frac{d\left(1+\frac{\theta_{s}T}{K}\right)}{\theta_{s}^{2}}\right)\left(H_{s}K\right)+S_{s}D\left(\frac{(b-T_{s})^{2}}{2b}\right)}
$$
\n
$$
E(TCT(T,K))=-\frac{T+\left(\frac{(b-T_{s})^{2}}{2b}\right)}{T+\left(\frac{(b-T_{s})^{2}}{2b}\right)}
$$
\n(9)

The non production period (T_d) is equal with total time minus production period. So the non production period can be modeled as:

$$
T_d = 1 - \frac{wT}{K} \tag{10}
$$

Substitute (4) to (10), one has;

$$
T_d = 1 - \frac{(d + \theta_v)T}{P} \tag{11}
$$

Substitute (11) to (9), one has:

Substitute (11) to (3), the has.
\n
$$
Cs + ((d + \theta_{\nu})T - mk) \frac{H_{\nu}}{\theta_{\nu}} + CtK \left(\frac{d\left(2 + \frac{\theta_{b}T}{K} \right)}{\theta_{b}^{2} \left(2 - \frac{\theta_{b}T}{K} \right)} - \frac{d\left(1 + \frac{\theta_{b}T}{K} \right)}{\theta_{b}^{2}} \right) (H_{b}K)
$$
\n
$$
E(TCT(T, K)) = \frac{T + \left(\frac{b - \left(1 - \frac{(d + \theta_{\nu})T}{R} \right)^{2}}{2b} \right)^{2}}{T + \left(\frac{b - \left(1 - \frac{(d + \theta_{\nu})T}{R} \right)^{2}}{2b} \right)}
$$
\n
$$
T + \left(\frac{b - \left(1 - \frac{(d + \theta_{\nu})T}{R} \right)^{2}}{2b} \right)
$$
\n(12)

The optimal replenishment period is found by deriving (12) in term of *T* and set the value equal to 0, one has;

$$
\frac{dTCT(T, K)}{dT} = \begin{pmatrix}\n\frac{Sd\left(b - 1 + \frac{d + \theta_{v}}{p}\right)}{b} + \frac{H_{v}(d + \theta_{b})^{2}TK\left(K - \frac{(d + \theta_{v})K}{p} + 1\right)}{dK^{2}} \\
+ \left(\frac{d}{\theta_{b}K\left(2 - \frac{\theta_{b}T}{K}\right)} + \frac{d\left(2 + \frac{\theta_{b}T}{K}\right)}{\theta_{b}K\left(2 - \frac{\theta_{b}T}{K}\right)} - \frac{d}{K\theta_{b}}\right) \frac{KH_{b}}{T} \\
+ \left(\frac{2 + \frac{\theta_{b}T}{K}}{\theta_{b}^{2}\left(2 - \frac{\theta_{b}T}{K}\right)} - \frac{d\left(1 + \frac{\theta_{b}T}{K}\right)}{\theta_{b}^{2}}\right) \frac{KH_{b}}{T^{2}} \\
+ \left(\frac{2 + \frac{\theta_{b}T}{K}}{\theta_{b}^{2}\left(2 - \frac{\theta_{b}T}{K}\right)} - \frac{d\left(1 + \frac{\theta_{b}T}{P}\right)}{\theta_{b}^{2}}\right) \frac{KH_{b}}{T^{2}} \\
+ \left(\frac{2 + \frac{\theta_{b}T}{K}}{\theta_{b}^{2}\left(2 - \frac{\theta_{b}T}{K}\right)} - \frac{d\left(1 + \frac{\theta_{b}T}{K}\right)}{\theta_{b}^{2}}\right) \frac{KH_{b}}{T} \\
+ \left(\frac{2 + \frac{\theta_{b}T}{K}}{\theta_{b}^{2}\left(2 - \frac{\theta_{b}T}{K}\right)} - \frac{d\left(1 + \frac{\theta_{b}T}{K}\right)}{\theta_{b}^{2}}\right) \frac{KH_{b}}{T}\n\end{pmatrix} \cdot \left(\frac{1}{\left(T + \frac{(b - 1 + \frac{d + \theta_{v}}{P})\gamma^{2}}{2b}\right)}\right)^{2} = 0
$$
\n(13)

If the optimal production down time is bigger than the upper bound of the uniform distribution unavailable time, then lost sales will not occur. In this situation, equation (12) is not fulfilled. Equation (12) should be revised as follow:

$$
Cs + \left((d + \theta_v)T - mk \right) \frac{H_v}{\theta_v} + CtK + \left(\frac{d \left(2 + \frac{\theta_b T}{K} \right)}{\theta_b^2 \left(2 - \frac{\theta_b T}{K} \right)} - \frac{d \left(1 + \frac{\theta_b T}{K} \right)}{\theta_b^2} \right) (H_b K)
$$

$$
E(TCT_{NL}(T, K)) = \frac{T}{T}
$$
 (14)

The optimal replenishment time for total cost without lost sales can be found by deriving (14) in term of *T*, and one has:

$$
\frac{dTCT_{NL}(T,K)}{dT} = \begin{pmatrix}\n\frac{Sd\left(b - 1 + \frac{d^2\theta_V}{p}\right)}{b} + \frac{H_v(d + t_b)^2TK\left(K - \frac{(d^2\theta_V)K}{p} + 1\right)}{dK^2} \\
+ \left(\frac{d}{\theta_b K\left(2 - \frac{\theta_b T}{K}\right)} + \frac{d\left(2 + \frac{\theta_b T}{K}\right)}{\theta_b K\left(2 - \frac{\theta_b T}{K}\right)^2} - \frac{d}{K\theta_b}\right)\frac{KH_b}{T} \\
+ \left(\frac{\left(2 + \frac{\theta_b T}{K}\right)}{\theta_b^2\left(2 - \frac{\theta_b T}{K}\right)} - \frac{d\left(1 + \frac{\theta_b T}{K}\right)}{\theta_b^2}\right)\frac{KH_b}{T^2} \\
+ \left(\frac{L_b}{\theta_b^2\left(2 - \frac{\theta_b T}{K}\right)} + \frac{H_v(d + \theta_b)^2 T^2\left(K - \frac{(d + \theta_V)K}{P} + 1\right)}{2Kd} + \left(\frac{2 + \frac{\theta_b T}{K}}{\theta_b^2\left(2 - \frac{\theta_b T}{K}\right)} - \frac{d\left(1 + \frac{\theta_b T}{K}\right)}{\theta_b^2}\right)\frac{KH_b}{T}\n\end{pmatrix} + \left(\frac{2 + \frac{\theta_b T}{K}}{\theta_b^2\left(2 - \frac{\theta_b T}{K}\right)} - \frac{d\left(1 + \frac{\theta_b T}{K}\right)}{\theta_b^2}\right)\frac{KH_b}{T}\n\begin{pmatrix}\n\frac{1}{T}\n\end{pmatrix}^2 + \left(\frac{2 + \frac{\theta_b T}{K}}{\theta_b^2\left(2 - \frac{\theta_b T}{K}\right)} - \frac{d\left(1 + \frac{\theta_b T}{K}\right)}{\theta_b^2}\right)\left(1 + \frac{\left(b - 1 + \frac{d + \theta_V}{P}\right)T^2}{2b}\right)\n\end{pmatrix}
$$

The single-vendor single-buyer inventory model with uniformly distributed maintenance time can be solved using the following procedure:

Step 1 $\operatorname{Set} K = 1$

- Step 2 Calculate *T** by solving equation (13)
- Step 3 Calculate (12) using T^* from step 2. If T_d is less than *b*, go to step 4, otherwise *T** is found.
- Step 4 Find *T** by solving equation 15. If TUC(K* 1, T) > TUC(K*, T) < TUC(K* + 1,T), the optimal solution is found, otherwise $K = K + 1$ and go to step 2.

Results and Discussion

In this section, a numerical example is used to show how the model works. The parameters are setup cost (*Cs*) \$40/ set up, transportation cost (*Ct*) \$ 0.5/ delivery, production rate (*p*) 150 per unit time, demand rate (*d*) 80 per unit time, manufacture holding cost (*Hv*) \$ 5/unit/unit time, buyer holding cost (*Hb*) \$ 6/unit/unit time, buyer lost sales cost (*S*) \$ 12/unit, manufacture deteriorating rate (*θv*) 0.05/unit time, and buyer deteriorating rate (θ_b) 0.06/unit time. Manufacture unavailability time is uniformly distributed between 0 and 1. Due to complexity of the model, a closed form solution can not be derived and the model is solved using simple heuristic method using Maple software. The optimal total cost can be derived when replenishment period is small but larger than zero.

Figure 3 shows total cost in varies value of *T*, when *K* is equal to 3.

(15)

Table 1. The computational results for Uniform distribution unavailability time

Table 2. Sensitivity analysis for Uniform distribution unavailability time.

Decision	Lost sales $cost(S)$				
variables	9.6	10.8	12	13.2	14.4
K	20	19	18	17	16
T^*	0.552	0.515	0.483	0.456	0.432
Manf.Cost	67.86	73.03	78.06	82.97	87.79
Buyer Cost	124.98	131.76	138.00	143.81	149.22
Total Cost	192.84	204.79	216.06	226.78	237.01

Table 1 shows the computational results of the numerical example. The optimal total cost per unit time is derived when the number of delivery (*K*) is equal to 18. The optimal total cost per unit time is equal to \$ \$216.06 and the optimal production time is 0.483. Since the lost sales cost is one of the important parameters, then a sensitivity analysis is conducted in different value of lost sales cost (*S*). The sensitivity analysis results is shown in Table 2.

The sensitivity analysis shows that the lost sales cost significantly affect the optimal total cost. When the lost sales cost increase 20%, the optimal total supply chain cost increase 9.6%. The optimal total cost increase as the lost sales cost increase. The result is similar as many previous research. The optimal frequency of delivery and the optimal replenishment time decrease as the lost sales cost increase. Manufacture and buyer try to minimize their cost by reducing their replenishment time and the frequency of delivery. The total cost per unit time of manufacture and buyer increase as the lost sales cost increase. Since the buyer reducing his replenishment period, the manufacture cost per unit time increase. The manufacture cost per unit time increase 12,46% and the buyer cost per unit time increase 8.13% as the lost sales cost increase 20%. Percentage increasing cost per unit time of manufacture higher than percentage increasing cost per unit time of the buyer. However manufacture cost is less than the buyer cost. In the supply chain model, the supply chain leader gets more benefit in a supply chain. Manufacture should give compensation to the buyer to make the buyer buy more products from the manufacture and reducint manufacture cost per unit time.

Conclusion

In this paper, a deteriorating production inventory model for two echelons supply chain by considering unreliable production system is developed. Uniform distributions of machine unavailability time are considered in this research. A simple heuristic method is used to solve the model since a closed form

solution can not be derived. A numerical example and a sensitivity analysis are derived to verify the model. The sensitivity analysis shows that the total supply chain cost per unit time increase as the lost sales cost increase. Manufacture cost per unit time increase as the lost sales cost increase because the buyer tries to minimize his cost by redusing replenishment period. The research can be extended by considering some manufacture strategies to influence buyer to buy more productsin unreliable machine environment.

Acknowledgement

The work is supported by research grant from Indonesia Ministry of Education (Number: 25/SP2H/ PP/LPPM-UKP/II/2012)

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