

# Turnitin Originality Report

Processed on: 19-May-2020 15:26 WIB

ID: 1327617462

Word Count: 6526

Submitted: 1

mmsse By Iwan Sahputra

Similarity Index

14%

## Similarity by Source

Internet Sources: 14%  
Publications: 16%  
Student Papers: 0%

8% match (Internet from 07-Mar-2020)

<https://link.springer.com/article/10.1007%2Fs10965-014-0577-2>

4% match ("Proceedings of the 13th International Conference on Metal Forming", steel research international, 09/2010)

["Proceedings of the 13th International Conference on Metal Forming", steel research international, 09/2010](#)

3% match (Internet from 17-Jul-2018)

[https://www.researchgate.net/profile/Iwan\\_Sahputra](https://www.researchgate.net/profile/Iwan_Sahputra)

IOP PUBLISHING MODELLING AND SIMULATION IN MATERIALS SCIENCE AND ENGINEERING Modelling Simul. Mater. Sci. Eng. 20 (2012) 000000 (15pp) UNCORRECTED PROOF [Effects of temperature and strain rate on the deformation of amorphous polyethylene: a comparison between molecular dynamics simulations and experimental results](#) I H Sahputra and A T Echtermeyer Engineering Design and Materials Department, Norwegian University of Science and Technology-NTNU, Trondheim, Norway E-mail: iwan.h.sahputra@ntnu.no Received 3 December 2012, in final form 25 June 2013 Published Online at stacks.iop.org/MSMSE/20 Abstract Molecular dynamics simulations are used to investigate the effects of temperature and strain rate on the deformation of amorphous polyethylene. The simulations predict the effects of temperature and strain rate on the stress–strain responses, Young’s modulus and Poisson’s ratio similar to those observed in laboratory experiments performed by other researchers. The time–temperature superposition principle is applied to the Young’s modulus and Poisson’s ratio to form a master curve to address the discrepancies in strain rates between the simulations and the experiments. Differences in the numbers of monomers and chains, the degree of crystallinity and molecular orientation lead to discrepancies in the Young’s modulus and Poisson’s ratio between simulations and experiments. 1. Introduction [Molecular dynamics \(MD\) can](#) predict [material](#) properties [based on first principles](#), mainly [using](#) the atomistic forces between molecules. This approach could help

in the design of new materials by modelling the behaviour of materials with altered molecular structures. The user could predict material performance under different loads and environments without performing traditional physical experiments in the laboratory. MD modelling of polymers has not yet reached this level. Current computational power is not sufficient to model the many macromolecules in polymeric materials and describe all the interactions within a reasonable time frame. This particularly applies to the modelling of long-term properties such as creep and fatigue. This paper investigates as to what extent temperature and strain rate effects can be described by MD. In particular, we investigate the possibility of using the time-temperature superposition 0965-0393/12/000000+15\$33.00 © 2012 IOP Publishing Ltd Printed in the UK & the USA 1 JNL: MSMS PIPS: 455170 TYPE: PAP TS: NEWGEN DATE: 30/7/2013 EDITOR: TT SPELLING: UK principle. High-density polyethylene (HDPE) is used for this investigation. HDPE has a simple molecular structure, even though it has amorphous and crystalline phases, and this polymer is employed [in a wide range of demanding industrial applications](#), for example [in gas distribution pipes](#) [1]. Several MD [studies have been performed to investigate the behaviour of](#) polyethylene (PE). Brown and Clark [2] modelled a single linear polymer containing 1000 monomers of PE in tension, performing simulations at different loading rates and temperatures. By qualitative comparison, they observed similar stress-strain responses between the simulations and laboratory measurements carried out at much lower strain rates. Yang et al [3] presented simulations of 1500 atoms of PE arranged in five chains of equal length. Their simulation produced a similar Young's modulus value as reported by Brown and Clark [2]. However, the simulated yield stress/strain and the ultimate strength predicted by these simulations were much higher than those obtained from laboratory experiments at a strain rate approximately six orders of magnitude smaller. Capaldi et al [4] used non-equilibrium MD simulations to simulate four chains with 1000 beads representing PE monomers at a variety of temperatures and strain rates. They found that their simulations were able to qualitatively reproduce the experimentally observed stress-strain behaviour of polymer glasses during compressive deformation. They also demonstrated that the simulated modulus is consistent with the experimentally determined modulus, but the yield stress was much higher. Rottler and Robbins [5] studied the [effect of temperature and strain rate on](#) shear yielding [of amorphous](#) glassy solids. A bead-spring model was used for non-particular polymers and the other model was a binary mixture composed of two particles. Both models were subjected to tensile or compressive strains with strain rates much higher than typical experimental tests. They found that the maximum shear yield stress drops linearly with increasing temperature and the dependence on strain rate can be described by either a logarithm or a power law added to a constant. Mahajan and Basu [6] investigated the effects of sample preparation, quench rate, sample size and strain rate on the ensemble and stress-strain response. They used a force field and mass of atoms that closely resembles that of PE and performed uniaxial compression simulations. They showed the sample preparation and simulation procedures, which were able to produce realistic stress-strain curves with strain rates much higher compared with the experimental tests. Lyulin et al [7] used united-atom models to simulate uniaxial deformation of low-molecular weight isopropylbenzene (iPB), brittle atactic polystyrene (PS) and tough bisphenol A polycarbonate (PC). After the deformation simulation at room temperature, they found the Young's modulus and yield stress values close to the typical value obtained from the experimental results at the same temperature; however, [there was huge discrepancy in the strain rates](#). These previous results indicate that MD is a useful tool to qualitatively investigate the relationship between micro-scale phenomena and macro-scale mechanical properties and, to some extent, to quantitatively determine these terms. However, there is a huge discrepancy between the simulated and laboratory strain rates. Because of the computational cost and time required, MD simulations typically use strain rates about six to ten orders of magnitude larger than the highest strain rates commonly used in laboratory experiments. This study will [investigate the effects of temperature and strain rate on the deformation](#) mechanisms [of amorphous](#) PE using MD [simulations](#). This investigation will further explore the

ability of MD simulations to serve as a tool, not only to produce results that are qualitatively similar to experimental results, but also to provide quantitative results. This is done by 2 Table 1. Functional forms and parameters for molecular potential energy. Interaction Functional form Parameters Bond stretch [Bond angle](#) bend [Dihedral angle](#) [torsion van der Waals](#)  $V_b = k_b(r_b - r_o)^2$   $V_a = k_a(\theta_a - \theta_b)^2$   $V_d = \sum_{\phi} k_n \cos^n \phi$   $V_{\phi} = \sum_{i,j} k_{ij} \cos^2 \phi_{ij}$   $V_{ij} = 4\epsilon_{ij} (r_{ij} - r_{ij}^*)^{-12} - \epsilon_{ij} (r_{ij} - r_{ij}^*)^{-6}$   $V_{ij} = 4\epsilon_{ij} (r_{ij} - r_{ij}^*)^{-12} - \epsilon_{ij} (r_{ij} - r_{ij}^*)^{-6}$   $r_{ij} - r_{ij}^* < r_c = 0$  or  $r_c > 0$   $k_b = 350 \text{ kcal mol}^{-1}$   $r_b = \text{bond length}$   $r_o = \text{equilibrium bond length} = 1.53 \text{ \AA}$   $k_a = 60 \text{ kcal mol}^{-1}$   $\theta_a = \text{bond angle}$   $\theta_b = \text{equilibrium bond angle} = 109.5^\circ$   $K_1 = 1.73 \text{ kcal mol}^{-1}$ ,  $K_2 = -4.49 \text{ kcal mol}^{-1}$   $K_3 = 0.776 \text{ kcal mol}^{-1}$ ,  $K_4 = 6.99 \text{ kcal mol}^{-1}$   $\phi_d = \text{dihedral angle}$   $\epsilon_{ij} = 0.112 \text{ kcal mol}^{-1}$ ,  $\sigma_{ij} = 4.01 \text{ \AA}$   $r_c = 10 \text{ \AA}$  comparing the dependence of the simulated Young's modulus and Poisson's ratio [on the temperature and strain rate](#) with [the dependences observed in laboratory experiments performed by other researchers](#). [Discrepancies in strain rates between simulations and laboratory experiments](#) will be discussed. 2. Model and simulation procedure Pure PE consists of alkanes, and its chemical formula is  $(\text{CH}_2)_n$ , where  $n$  is the degree of polymerization or the number of ethylene monomers. The typical degree of polymerization of PE is between 100 and 250 000 or more. The molecular weight of PE is 14.02 per monomer. A PE sample [consists of a large number of chains](#) with [a range of different lengths](#). HDPE has the chemical structure closest to pure PE because it consists primarily of unbranched PE molecules compared with other types of PE such as low-density polyethylene (LDPE). The [united-atom approach](#) was used [to model the amorphous PE system. This approach simplifies each CH<sub>2</sub> monomer as a single monomer](#) particle and has been used by several researchers [2–4]. The DREIDING force field [8] was used to simulate the interaction between monomers. In DREIDING, the potential energy of a molecule consists of the combined energies of bonded interactions (bond stretching, bond angle bending and dihedral angle torsion) and non-bonded interactions (van der Waals interactions, represented by the Lennard-Jones potential). The functional forms and parameters [9, 10] of the DREIDING force field are presented in table 1. The initial amorphous PE sample was generated using Monte Carlo self-avoiding random walks similar to previously developed methods [10]. The [basic idea of this method is each monomer is placed on each site of the face-centred cubic \(fcc\) lattice with a lattice constant of 1.53 \AA. The initial position is randomly selected and the next atom is placed according to the probability for each possible bond angle direction and the density of unoccupied neighbour sites.](#) The sample [contains ten chains, each consisting of 1000 monomers](#). An MD program designed for parallel computers, LAMMPS [11], was used to equilibrate the initial sample structure and simulate the deformation process. All the simulations were performed on the 'Njord' IBM p575+ super computer system at NTNU. This simulation represents the most complex simulation that can be performed on our supercomputer within a reasonable time frame, but [it is a very small sample compared with real PE](#). 3 Figure 1. Distribution of the bond length, bond angle and dihedral angle after the final equilibration stage at a temperature of 200 K. The simulation method used here followed that in [10]. [Initial velocities were assigned to the atoms by randomly selecting from a uniform distribution at a temperature of 500 K. Before the](#) deformation process, the system was equilibrated using a Langevin thermostat as described in [12] for 10 picoseconds (ps) at 500 K. The Langevin thermostats follow the Langevin equation of motion, where a frictional force proportional to the velocity is added to the conservative force, adjusting the kinetic energy of the particle so that the temperature matches the set temperature [13]. This thermostat was used within NVE [ensembles to perform Brownian dynamics simulation of the melted polymer. The system was then equilibrated at constant particle number, pressure and temperature \(NPT ensembles\) for 25 ps at 500 K and then cooled to the desired temperature](#) (100, 200, 250 and 350 K) for 25 ps. The final equilibration stage was carried out for NPT ensembles at the desired temperatures for 25 ps. The [NPT ensembles were performed using a Nose-Hoover thermostat and a barostat coupled to the atom velocities and simulation box dimensions. The time integration of the motion equations was performed using the time-reversible measure-preserving Verlet and rRESPA integrators. Periodic boundary conditions were applied to all directions of the](#)

simulation box. During the sample preparation processes, pressure and stress were monitored to characterize whether equilibration has been satisfied. In the final equilibration stage, all the potential energies (bond, angle, dihedral and van der Waals) and polymer chain geometries were also monitored to check whether the final equilibrium was reached and the sample was ready to be deformed. Figure 1 shows an example of the polymer chain geometry after the final equilibration stage at a temperature of 200 K. The mean value of bond length is 1.529 Å with a standard deviation of 0.023 Å, while the mean value of bond angle is 109.29° with a standard deviation of 3.393°. These mean values are slightly lower than the equilibrium values of the potential parameters for bond length and angle, which are 1.53 Å and 109.5°, respectively. The dihedral angles are distributed around trans and gauche states, centred around 66° and 180°. The distributions are similar to those in other MD simulations of PE [6, 10]. A polymer's size can be characterized by the end-to-end distance,  $r$ , or the radius of gyration. For the freely jointed chain model, the end-to-end distance,  $r$ , is proportional to the bond length,  $l$ , and to the square root of the number of bonds,  $n$ . The characteristic ratio is defined as  $C = n l^2 \langle r^2 \rangle^{-1}$ . (1) In the freely jointed PE chain,  $C = 1$ , in the freely rotating chain,  $C = 2$ , and in the hindered rotation chain,  $C = 3.4$  [14]. For real PE, the characteristic ratios are estimated from direct intrinsic viscosity measurements to be 7.10, 6.99 and 6.80 at temperatures of 127.5 °C, 142.2 °C and 163.9 °C, respectively [15]. In more recent light scattering measurements on linear PE in diphenyl at 400 K (= 127 °C), characteristic ratios from 8.7 to 10.5 were found [16]. The sample of this study, after being equilibrated at a temperature of 500 K (= 227 °C) has a characteristic ratio,  $C$ , of 3.4. This indicates that the simulation sample is composed of more tightly coiled chains compared with the real PE. The accuracy of the stress-strain response of glassy polymers with MD simulations depends on the characteristic ratio,  $C$  [6]. However, the accuracy of  $C$  is especially important for the stress-strain response after the yield stress and for the slope of the rehardening part. The initial low strain is not influenced significantly by the value of  $C$ . As the focus of this study is on the Young's modulus and Poisson's ratio calculated at a low strain (0.02% or 2%), only the initial deformation responses of the simulations are used to calculate the elastic properties. For this reason, the model is considered adequate for studying elastic properties at low strains. However, this model is not an adequate model to predict properties beyond the elastic limit, such as the yield stress, softening and hardening, which is typically also beyond the practical application of polymers. Deformation was simulated by changing the simulation box in one longitudinal direction during a dynamic run. The other two transverse directions of the box had zero applied pressure, allowing the box to contract sideways. The change in longitudinal dimension occurred at a constant engineering strain rate. The tensile strain is unitless and is defined as the length change divided by the original box length. For each combination of temperature and strain rate, three simulations were performed to calculate the Young's modulus and Poisson's ratio. In each of the three simulations, the system was either elongated in the X, Y or Z direction and the obtained Young's modulus and Poisson's ratio were averaged. This was done because the initial structure and velocities were randomly generated, and after the equilibrium processes, the system could have different morphological configurations. This is similar to the practice of using several samples in laboratory experiments to ensure that the results are statistically representative of the material properties, which could vary.

### 3. Results and discussion

#### 3.1. Effects of temperature and strain rate on the stress-strain curve and volume strain

Figure 2 presents typical stress-strain curves obtained from the simulations performed in this study. The simulations were conducted using a strain rate of 109 s<sup>-1</sup> at a temperature of 200 K. The stress-strain curves were obtained from three simulations in which the sample was elongated in the X, Y or Z direction in each simulation. The heterogeneity and small size of the sample produced noisy stress-strain curves and therefore polynomial smoothing was used to reduce the fluctuation of the stress. This was done by applying the polynomial equations to the original stress-strain data and by calculating the least-squares fit through the data points. The three curves are close to each other at a low strain. At a higher strain, above

approximately 0.2% or 20%, the curves demonstrate that the stress–strain responses of the sample differ depending on the direction of elongation. This is due to the anisotropy of the structure of the polymer chain in the small sample modelled here. As the focus of this study is on the Young’s modulus and Poisson’s ratio calculated at a low strain (0.02 or 2%), similar initial deformation responses of the simulations in three different directions could be used to calculate the elastic properties. But this small model is not an adequate model to simulate large strain beyond the elastic limit, which is typically also beyond the practical application 5 Figure 2. Stress–strain curves of three simulations elongated in the X, Y or Z direction at a strain rate of 109 s<sup>−1</sup> at 200 K. The main focus in this study is on the initial strain range up to about 0.02% or 2%. of polymers. For the following discussion in this section, only stress–strain curves from the deformation along the X-direction will be shown. The curve for X-direction elongation in figure 2 has the same typical shape as those obtained from laboratory experiments on PE, for instance the experiments using strain rates between 10<sup>−4</sup> and 10<sup>−2</sup> s<sup>−1</sup> performed by Hiss et al [17] and Addiego et al [18]. However, there is a significant difference in yield stress between experiments and simulations. Yield stress is defined here as the first stress point on the stress–strain curve where an increase in strain occurs without an increase in stress. The experimentally obtained yield stresses are between 20 and 30 MPa while in this simulation they are about 120 MPa. This is the same order of magnitude as found in other simulations, for instance [2–4]. As the yield stress increases with the strain rate, the simulations are expected to produce a higher yield stress than the experiments. The effect of the strain rate is presented in figure 3 and is limited to deformation at the strain of 0.02% or 2% for calculating [the Young’s modulus and Poisson’s ratio](#). The [simulations](#) show Hookean elasticity responses to the applied uniaxial load at low strains. Figure 3 indicates that the stiffness and yield stress increase with increasing strain rate. Hiss et al [17] and Addiego et al [18] also found that increasing strain rate increases the yield [stress](#). [Figure 4](#) presents the [influence of temperature on](#) the stress–strain behaviour. Decreasing temperature increases the stiffness and the yield stress. The Young’s modulus and Poisson’s ratio values discussed in the following sections were obtained by averaging the values calculated from the stress–strain curves from the three simulations, in which the sample was elongated in the X, Y or Z direction in each simulation. The average values for [different strain rates and temperatures are shown in](#) table 2 together with the standard deviations. The standard deviations are reasonably low.

### 3.2. [Effects of temperature and strain rate on the Young’s modulus](#)

The Young’s modulus was calculated from the slope of the stress–strain curve below the linear limit, typically below a strain of 0.02% or 2%. For each combination of temperature and strain 6 Figure 3. Effect of strain rate on the stress–strain curve at 200 K. [Figure 4. Effect of temperature on](#) the stress–strain curve at a strain rate of 1010 s<sup>−1</sup>. rate, the Young’s modulus values were obtained from three simulations and averaged. Table 2 [shows the average value and standard deviation](#). Figure 5 presents [the](#) average value of the Young’s modulus as a function of temperature and strain rate. Sigmoid curve fitting equations were applied to these average values to show the trend of the Young’s modulus as a function of temperature. Figure 5 indicates that the Young’s modulus decreases with increasing temperature in all simulations. This dependence of stiffness on temperature has also been observed for other polymers, for instance by Mahieux and Reifsnider [19] and Richeton et al [20]. The results 7 Table 2. [Young’s modulus and Poisson’s ratio](#) calculated from the [simulations](#).

Strain rate (s <sup>−1</sup> )	Temperature (K)	Average Young’s modulus (GPa)	Standard deviation	Poisson’s ratio														
1011	100	200	250	350	5.457	3.313	1.846	0.579	0.404	0.961	0.030	0.195	0.283					
0.277	0.269	0.265	0.025	0.022	0.017	0.005	1010	100	200	250	350	3.198	2.069	1.438	0.608	0.200	0.278	0.319
0.146	0.326	0.327	0.339	0.416	0.051	0.034	0.042	0.041	109	100	200	250	350	2.334	1.765	1.172	0.429	0.233
0.106	0.139	0.192	0.374	0.397	0.451	0.482	0.061	0.042	0.025	0.107	108	100	200	250	350	1.609	1.349	0.625
0.161	0.199	0.147	0.005	0.069	0.385	0.435	0.504	0.495	0.025	0.025	0.083	0.125	Figure 5. Effect of strain rate and temperature on Young’s modulus. also show that the simulation using a higher strain rate produces a higher Young’s					

modulus compared with the simulation using a slower rate. The results produced by the highest strain rate simulations ( $10^{11} \text{ s}^{-1}$ ) require careful attention. This strain rate is close to the vibrational frequency of PE, which is between  $1.53 \times 10^{12}$  and  $8.76 \times 10^{13} \text{ s}^{-1}$  according to [21]. Strain rates close to the vibrational frequencies may lead to errors in the molecular trajectories, with the result that the system may no longer have a normal structure. In each time step of the deformation process, the atomic positions are remapped following the change in the size of the simulation box at a constant strain rate. The changes of the atomic positions could be sufficiently large compared with the atomic oscillations, resulting in a discontinuous jump in the molecular bond distance without any physical meaning. Therefore, the  $10^{11} \text{ s}^{-1}$  simulation results will not be used in the subsequent analysis and discussion. It is well known that the mechanical properties of polymers vary with both time and temperature. As indicated in figure 5, increasing the temperature affects the Young's modulus in a similar way as decreasing the strain rate. The time-temperature superposition based on this phenomenon is widely used to form a 'master curve' using a shift factor to superimpose mechanical properties measured at different temperatures. Experimental test results, such as the Young's moduli, are multiplied by a shift factor to produce a single master curve. The shift factor is determined experimentally with respect to a reference temperature. The shift factor used to construct a master curve was experimentally determined for a large number of amorphous polymers by Williams, Landel and Ferry [22], who expressed the WLF equation:  $\log_{10} a_T = C_2 + (T - T_0) - C_1(T - T_0)$ . (2) Equation (2) is an empirical equation found as an approximately identical shift factor-temperature relation for a wide variety of polymers, polymer solutions, organic glass-forming liquids and inorganic glasses. The theoretical basis to this equation is Doolittle's free volume [23] that is based on experimental data. The temperature dependence of viscosity arises largely from its dependence on free volume. The free volume is constant up to  $T_g$  and then increases linearly with increasing temperature. Equation (2) has been validated with higher strain rates than typical experimental test rates [24, 25]. But the strain rates were still much lower than typical MD simulation rates. Equation (2) is valid above the glass transition temperature ( $T_g$ ) because below this temperature,  $\log a_T$  increases less rapidly with decreasing temperature [22]. Using the WLF equation at much higher strain rates than used in laboratory experiments is an unproven approach, but as discussed later it can explain results from MD fairly well. The values of the WLF constants  $C_1$  and  $C_2$  for these simulations were taken to be 15.0 and 50.5, respectively, from [26]. They were calculated using experimental results of an HDPE sample. The sample's  $T_g$  ( $= 155 \text{ K}$ ) was chosen as the reference temperature  $T_0$ . Since our sample in the simulations was purely amorphous PE, the WLF constants for the HDPE sample with the lowest degree of crystallinity (40%) in [26] were chosen to be used for the calculation of the shift factor for our simulation results. Bauwens et al [27] reported that the yield stress of glassy polymers below  $T_g$  can be described by the Eyring theory of non-Newtonian flow. The linear form of the Eyring equation is similar to the Arrhenius activation energy equation. The shift factor is given by  $\log_{10} a_T = 2.303R/Q [1/T - 1/T_0]$  (3) where Q is the activation energy and R is the universal gas constant. The activation energy of linear PE is taken from [28] as  $27 \text{ kJ mol}^{-1}$ . The Young's modulus values at different temperatures and strain rates obtained from the simulations were plotted against the shifted log strain rate from equation (2) for data at the temperature above  $T_g$  and from equation (3) for data at the temperature below  $T_g$ . The master curve at  $T_g$  ( $155 \text{ K}$ ) is presented in figure 6. This figure shows that the original log strain rate between 8 and 10 has been shifted to between about  $-4$  and  $5$ . This indicates that the simulations predict Young's modulus behaviour in accordance with the time-temperature superposition principle. Young's moduli calculated from the simulation results were compared with the values obtained by experimental measurements reported by Bucknall [29]. In his report, the Young's modulus was measured from HDPE samples using tensile tests over a range of strain rates and at different temperatures. The Young's modulus was found to increase with increasing strain rate. Figure 6. Master curve (dashed line) of Young's modulus. Figure 7. Comparison of Young's modulus as a function of strain rate

from measurements by Bucknall [29] and the master curve (dashed line) of the simulation at  $T_g$  (155 K). rate and decreasing temperature. Figure 7 compares measurements by Bucknall [29] and the master curve obtained from the simulations. The WLF equation, equation (2), was again applied to the Young's modulus values of Bucknall [29] to form a master curve. The values of the constants  $C_1$  and  $C_2$  for the previous WLF equation could not be used because the samples studied by Bucknall [29] have degrees of crystallinity between 94% and 97%. Therefore, the  $C_1$  and  $C_2$  constants were assigned values of 8.86 and 101.6 based on [22], and the reference temperature ( $T_0$ ) was set to 233 K. Over a range of temperatures between  $T_g$  and  $T_g + 100$ , these values are valid for a wide variety of polymers, polymer solutions, organic glass-forming liquids and inorganic glasses [22]. 10 Figure 8. Comparison of the master curve of Bucknall [29] at 233 K (solid line) and the master curve of the simulation at 155 K (dashed line). Figure 8 compares the master curve found by Bucknall with the simulation. The Young's moduli of these simulations are lower than those of the experiments, but the master curves have similar shapes. HDPE has a high degree of crystallinity and a varying amount of amorphous structure. The elastic modulus increases approximately in proportion to the degree of crystallinity in a certain range [30–32]. In this simulation, the PE system is purely amorphous, while the HDPE in Bucknall's report has a degree of crystallinity between 94% and 97% as measured by Pranadi and Manuel [33]. According to Popli and Mandelkern [32], for degrees of crystallinity less than 25%, the moduli remain constant at approximately 20 MPa. Therefore, the degree of crystallinity leads to a difference in the Young's modulus between experimental measurements and the simulated results. Semicrystalline PE has not only a crystalline region surrounded by a disordered (amorphous) region, but also an interfacial region that connects the two. Therefore, the elastic modulus will be affected both by the degree of crystallinity and by how the interfacial region connects the crystalline and amorphous regions. Another possible reason for the discrepancy between the simulations and experimental measurements is the effect of molecular orientation. HDPE elongated in the solid state exhibits a strong dependence of the Young's modulus on molecular orientation, for instance as reported by Capaccio and Ward [34] and Capaccio et al [35]. Increasing the degree of orientation increases the Young's modulus. The experimental samples studied by Bucknall [29] were prepared by an injection moulding process and could have had higher degree of molecular orientation compared with the simulated samples.

### 3.3. Effects of temperature and strain rate on Poisson's ratio

In each simulation, a curve of transverse strain versus longitudinal strain was obtained and Poisson's ratio was calculated from the slope of the curve at a low strain. For each combination of temperature and strain rate, the Poisson's ratio values were obtained from three simulations 11 Figure 9. Effects of temperature and strain rate on Poisson's ratio. Figure 10. Master curve (dashed line) of Poisson's ratio. and averaged. Table 2 [shows the average value and standard deviation](#). Figure 9 presents [the average value](#) of Poisson's ratio as a function of temperature and strain rate. Again, the sigmoid curve fitting equations were applied to these average values to show the trend of Poisson's ratio as a function of temperature. Figure 9 indicates that in the simulations using strain rates of 108, 109 and 1010  $s^{-1}$ , Poisson's ratio increases with temperature following a sigmoidal trend. This trend is similar to the experimental results of other polymers reported by Seitz [36] for PC, PS, PMMA, PVT, ST/MMA, PVC and POMS; by Mott et al [37] for PS and PMMA; by Pandini and Pegoretti [38] for PBT and by Pandini and Pegoretti [39] for epoxy resins. Poisson's ratio depends on the strain rate and temperature, as indicated in figure 9. In the same way as for the Young's modulus, equation (2) was used to calculate the log shift factor for Poisson's ratio at the temperature above  $T_g$  and equation (3) was used for the temperature below  $T_g$ . The Poisson's ratio master curve is presented in figure 10. These simulations are 12 Figure 11. Comparison of Poisson's ratio from data measured by Bilgin et al [40], Waterman [41] and the simulation model. able to produce the trend in Poisson's ratio following the time (or strain rate)–temperature superposition principle. Poisson's ratios obtained from the simulation results were compared with experimental measurements. Bilgin et al [40] found that Poisson's ratio of the MDPE pipe at a strain

rate close to  $1000 \mu\text{e min}^{-1}$  (approximately  $1.6 \times 10^{-5} \text{ s}^{-1}$ ) increased from 0.42 at  $-6.7 \text{ }^\circ\text{C}$  to 0.48 at  $49 \text{ }^\circ\text{C}$ . The equation of the curve fit to the simulation at a strain rate of  $109 \text{ s}^{-1}$  in figure 10 showed that Poisson's ratio was 0.464 at a temperature of  $-6.7 \text{ }^\circ\text{C}$  (approximately 266 K), and 0.481 at  $49 \text{ }^\circ\text{C}$  (approximately 322 K). Waterman [41] calculated the complex Poisson's ratio of six different samples of PE by measuring the velocity and attenuation of ultrasonic longitudinal and transverse pulses at a frequency of 5 MHz and a strain rate of approximately  $102 \text{ s}^{-1}$ . For comparison with the simulations, we used the real part of the complex Poisson's ratios of these measurements because the value of the real part is close to the time-dependent Poisson's ratio [42]. At  $-80 \text{ }^\circ\text{C}$ , the experimental value of Poisson's ratio was 0.35, and at  $50 \text{ }^\circ\text{C}$  it was 0.47. In the simulations, Poisson's ratio was 0.39 at  $-80 \text{ }^\circ\text{C}$  (approximately 193 K) and 0.48 at  $50 \text{ }^\circ\text{C}$  (approximately 323 K). Figure 11 presents [a comparison](#) between [the simulation](#) and the [experimental](#) values [of Poisson's ratio](#). [Figure 11 shows](#) that the trends [of the](#) effects of strain rate and temperature on Poisson's ratio in the simulations are similar to those in the experiments. The difference between Poisson's ratios measured experimentally and calculated in the simulations results from the same factors that influence the Young's modulus as discussed in the previous section.

#### 4. Conclusion

Molecular dynamics simulations of the deformation of amorphous PE are performed at various engineering strain rates and temperatures. Comparisons of the [effects of temperature and strain rate on the](#) deformation [responses](#) between MD simulations [and](#) laboratory experiments are 13 presented and discussed. The stress-strain curves at a low strain obtained from the simulations have the same typical shapes as those obtained from laboratory experiments. The Young's modulus and Poisson's ratio values were calculated from the simulations showing the strain rate and temperature dependences and were in reasonable agreement with the experimental measurements. The time (or strain rate)-[temperature superposition principle](#) was [applied to the Young's modulus and Poisson's ratio to form master](#) curves. These master curves can be used to bridge the difference between the high strain rates of the simulations and the much lower rates of the laboratory experiments. The differences in terms of the [numbers of monomers and chains,](#) [the degree of crystallinity and](#) the [molecular orientation lead to discrepancies](#) between [the Young's modulus and Poisson's ratio](#) values calculated from the simulations and those measured in laboratory experiments.

AQ1

References [1] ISO/TS 10839:2000, Polyethylene pipes and fittings for the supply of gaseous fuels—code of practice for design, handling and installation [2] Brown D and Clarke J H R 1991 Molecular dynamics simulation of an amorphous polymer under tension: I. Phenomenology *Macromolecules* 24 2075–82 [3] Yang L et al 1997 Extended ensemble molecular dynamics method for constant strain rate uniaxial deformation of polymer systems *J. Chem. Phys.* 107 4396–407 [4] Capaldi F M et al 2004 Molecular response of a glassy polymer to active deformation *Polymer* 45 1391–9 [5] Rottler J and Robbins M O 2003 Shear yielding of amorphous glassy solids: effect of temperature and strain rate *Phys. Rev. E* 68 011507 [6] Mahajan D K and Basu S 2010 On the simulation of uniaxial, compressive behaviour of amorphous, glassy polymers with molecular dynamics *Int. J. Appl. Mech.* 02 515–41 [7] Lyulin A V et al 2006 Atomistic simulation of bulk mechanics and local dynamics of amorphous polymers *Macromol. Symp.* 237 108–18 [8] Mayo S L et al 1990 DREIDING: a generic force field for molecular simulations *J. Phys. Chem.* 94 8897–909 [9] Lavine M S et al 2003 Molecular dynamics simulation of orientation and crystallization of polyethylene during uniaxial extension *Polymer* 44 1771–9 [10] Hossain D et al 2010 Molecular dynamics simulations of deformation mechanisms of amorphous polyethylene *Polymer* 51 6071–83 [11] Plimpton S J 1995 Fast parallel algorithms for short-range molecular dynamics *J. Comput. Phys.* 117 1–19 [12] Schneider T and Stoll E 1978 Molecular-dynamics study of a three-dimensional one-component model for distortive phase transitions *Phys. Rev. B* 17 1302 [13] Adelman S A and Doi J D 1976 Generalized Langevin equation approach for atom-solid-surface scattering— general formulation for classical scattering off harmonic solids *J. Chem. Phys.* 64 2375–88 [14] Gedde U W 1995 *Polymer Physics* (London: Chapman and Hall) [15] Nakajima A et al 1967 Unperturbed chain dimensions of



polyethylene in theta solvents J. Polym. Sci. C 15 285–94 [16] Muraoka Y et al 1983 Direct determinations of the unperturbed dimensions of linear polyethylene molecules Br. Polym. J. 15 107–9 [17] Hiss R et al 1999 Network stretching, slip processes, and fragmentation of crystallites during uniaxial drawing of polyethylene and related copolymers. A comparative study Macromolecules 32 4390–403 [18] Addiego F et al 2006 Characterization of volume strain at large deformation under uniaxial tension in high- density polyethylene Polymer 47 4387–99 [19] Mahieux C A and Reifsnider K L 2001 Property modeling across transition temperatures in polymers: a robust stiffness–temperature model Polymer 42 3281–91 [20] Richeton J et al 2005 A unified model for stiffness modulus of amorphous polymers across transition temperatures and strain rates Polymer 46 8194–201 [21] Barrera G D et al 2006 The vibrational spectrum and ultimate modulus of polyethylene Macromolecules 39 2683–90 [22] Williams M L et al 1955 The temperature dependence of relaxation mechanisms in amorphous polymers and other glass-forming liquids J. Am. Chem. Soc. 77 3701–7 14 [23] Doolittle A K 1951 Studies in Newtonian flow: II. The dependence of the viscosity of liquids on free-space J. Appl. Phys. 22 1471–5 [24] Zhao J, Knauss W G and Ravichandran G 2007 Applicability of the time–temperature superposition principle in modeling dynamic response of a polyurea Mech. Time-Depend. Mater. 11 289–308 [25] Rauh A et al 2012 Application of the time–temperature superposition principle to the mechanical characterization of elastomeric adhesives for crash simulation purposes Eur. Phys. J. Spec. Top. 206 15–24 [26] Alberola N et al 1992 Mechanical  $\gamma$  and  $\beta$  relaxations in polyethylene: I. Glass transitions of polyethylene Eur. Polym. J. 28 935–48 [27] Bauwens J C et al 1969 Tensile yield-stress behavior of poly(vinyl chloride) and polycarbonate in the glass transition region J. Polym. Sci. A-2 7 1745–54 [28] Stadler F J et al 2008 Thermorheological behavior of various long-chain branched polyethylenes Macromolecules 41 1328–33 [29] Bucknall C B 1986 Application of fracture mechanics to the prediction of the ductile-brittle transition Pure Appl. Chem. 58 999–1014 [30] Peacock A J and Mandelkern L 1990 The mechanical properties of random copolymers of ethylene: force–elongation relations J. Polym. Sci. B 28 1917–41 [31] Kennedy M A et al 1994 Tensile properties of crystalline polymers: linear polyethylene Macromolecules 27 5297–310 [32] Popli R and Mandelkern L 1987 Influence of structural and morphological factors on the mechanical properties of the polyethylenes J. Polym. Sci. B 25 441–83 [33] Pranadi H and Manuel A J 1980 Application of wide line nuclear magnetic resonance to the determination of the crystallinities of isotropic polyethylenes Polymer 21 303–8 [34] Capaccio G and Ward I M 1975 Ultra-high-modulus linear polyethylene through controlled molecular weight and drawing Polym. Eng. Sci. 15 219–24 [35] Capaccio G et al 1975 Preparation of ultra-high modulus linear poly-ethylenes: effect of initial crystallization conditions Polymer 16 469 [36] Seitz J T 1993 The estimation of mechanical properties of polymers from molecular structure J. Appl. Polym. Sci. 49 1331–51 [37] Mott P H, Dorgan J R and Roland C M 2008 The bulk modulus and Poisson’s ratio of ‘incompressible’ materials J. Sound Vib. 312 572–5 [38] Pandini S and Pegoretti A 2011 Time and temperature effects on Poisson’s ratio of poly(butylene terephthalate) eXPRESS Polym. Lett. 5 685–97 [39] Pandini S and Pegoretti A 2008 Time, temperature, and strain effects on viscoelastic Poisson’s ratio of epoxy resins Polym. Eng. Sci. 48 1434–41 [40] Bilgin O et al 2007 Thermal and mechanical properties of polyethylene pipes J. Mater. Civil Eng. 12 1043–52 [41] Waterman H A 1963 Determination of the complex moduli of viscoelastic materials with ultrasonic pulse method (part II) Kolloid-Z.u.Z.f. Polymere 192 9–16 [42] Tschoegl N W et al 2002 Poisson’s ratio in linear viscoelasticity—a critical review Mech. Time-Depend. Mater. 6 3–51 15 QUERIES Page 14 AQ1 Please check the details for any journal references that do not have a blue link as they may contain some incorrect information. Pale purple links are used for references to arXiv e-prints. Modelling Simul. Mater. Sci. Eng. 20 (2012) 000000 I H Sahputra [et al Modelling Simul. Mater. Sci. Eng. 20 \(2012\) 000000 I H Sahputra](#) [et al Modelling Simul. Mater. Sci. Eng. 20 \(2012\) 000000 I H Sahputra](#) [et al Modelling Simul. Mater. Sci. Eng. 20 \(2012\) 000000 I H Sahputra](#) [et al Modelling Simul. Mater. Sci. Eng. 20 \(2012\) 000000 I H Sahputra](#) [et al Modelling Simul. Mater. Sci. Eng. 20 \(2012\) 000000 I H Sahputra](#)

