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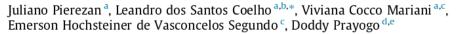
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Chaotic coyote algorithm applied to truss optimization problems





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ABSTRACT

The optimization of truss structures is a complex computing problem with many local minima, while metaheurist are naturally suited to deal with multimodal problems without the need of gradient information. The Coyote Optimiza on Algorithm (COA) is a population-based nature-inspired metaheuristic of the swarm intelligence field for global optimization that considers the social relations of the coyote proposed to single-objective optimization. Unlike most widespread algorithms, its population is subdivided in packs and the internal social influences are designed. The COA requires a few control hyperparameters including the number of packs, the population size, and the number maximum of generations. In this paper, a modified COA (MCOA) approach based on chaotic sequences generated by Tinkerbell map to scatter and association probabilities tuning and an adaptive procedure of updating parameters related to social condition is proposed. It is then validated by four benchmark problems of structures optimization including planar 52-bar truss, spatial 72-bar truss, 120-bar dome truss and planar 200 bar-truss with discrete design various and focus in minimization of the structure weight under the required constraints. Simulation results collected in the mentioned problems demonstrate that the proposed MCOA presented competitive solutions when compared with other state-of-the-art metaheuristic algorithms in terms of results quality.

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1. Introduction

Structural optimization is a subject that has gained the attention of researchers because of its dia and large applicability to the design of structures. Besides, the truss design is the most classical bend and in structural optimization [1–21]. Discrete optimization of truss structures is a hard computing problem with many local minima. Metaheuristic algorithms are naturally suited for discrete minimation problems as they do not require gradient information. Truss optimization may subject to static and dynamic constraints. Static constraints include structural kinematic stability, maximum allowable stress in truss members, maximum allowable deflection in the truss nodes and critical buckling load. However, dynamic constraints impose limits on the natural frequency of the desired truss to avoid the destructive resonance phenomenon. Taking both static and dynamic constraints into account

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the search space becomes non-convex and may subterfuge the solver trap in a local optimum.

Deplementation is more challenging in the categoric of discrete optimization problems such as several truss designs that usually entail a complex design space with multiple local optima. Also, several types of research have verified that the classical optimization methods based on gradient information involving the calculation of first and/or second derivatives are not efficient enough or always efficient in dealing with many larger-scale real-world multimodal, non-continuous, and non-differentiable problems [9]. To increasing the efficiency and accuracy of the optimization methods and to overcome the computational shortcomings of categoric nesearchers have encouraged to rely on metaheuristic optimization algorithms. The term metaheuristic describes higher-level heuristics that are proposed for the solution to a wide range of optimization problems.

Shih and Lee [10] applied the modified double-cuts approach for large-scale fuzzy optimization in 25-bar and 72-bar truss design problems. The proposed approach was better than the

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single-cut approach and easy programming. Several truss structures with discrete variables were solved by a hybrid particle swarm optimizer (PSO) with harmony search (HS) scheme, called (HPSO) by Li et al. [11]. The HPSO approach was validated and compared with the PSO and the PSO with the passive congregation being able to accelerate the convergence rate effectively. Degertekin and Hayalioglu [12] applied a teaching-learning-based optimization (TLBO) for optimization of truss structures. It obtained results as good as or better than the other metaheuristic algorithms in terms of both the optimum solutions and the convergence capability in most cases. A different approach named Ray optimization was applied to minimize the size, shape and weight of truss structures [13]. An adaptive dimensional search (ADS) was proposed for discrete truss sizing optimization problems [14]. The robustness of the ADS was investigated and verified using two benchmark examples as well as three real-world problems. When ADS was compared with other metaheuristic techniques indicates that it is capable of locating improved solutions using mud7 esser computational effort.

The mine blast algorithm (MBA), improved MBA (IMBA), and the water 14 cle algorithm (WCA) were applied for weight minimization 14 truss structures including discrete sizing variables, offering a good degree of competitiveness with other state-of-the-art metaheuristics [15]. A novel adaptive hybrid evolutionary firefly algorithm (AHEFA) was applied for shape and size optimization of truss structures under multiple frequency constraints. Accordingly, the convergence rate is significantly improved with high solution accuracy [16]. The authors Assimi and Ja 7 li [17] utilized the hybrid genetic programming algorithm for optimum connectivity table among the truss nodes, and optimal c 7 sectional areas subject to design constraints were considered both types of continuous and discrete design variables.

Degertekin and his collaborators [18] modified the Jaya Algorithm (JA) improving convergence speed and reducing the number of structural analyses required in the optimization process. Six classical weight minimization problems of truss structures including sizing, layout and large-scale optimization problems with up to 204 design variables were solved. Discrete sizing/layout variables and simplified topology optimization were considered. A novel Jaya Algorithm (JA) 61 s proposed by Degertekin et al. [19] for discrete optim 5 tion, denoted as discrete advanced JA (DAJA), and applied for truss structures under stress and displacement constraints. Results collected in seven benchmark problems demonstrated the superiority of DAJA over other state-of-the-art metaheuristic algorithms. The multi-objective colliding bodies optimization (MOCBO) algorithm was proposed by Kaveh and Mahdavi [20] and used to solve two truss structural bi-objective functions. The accuracy and efficiency of the optimization algorithm were compared with literature with promising performance.

An extension of the basic truss layout optimization using various materials was considered in [21]. A novel improved version of the particle swarm optimization algorithm (GEMPSO) was developed for solving six benchmark problems and three truss structures with two multi-material layouts, showing that the appropriate use of expensive stronger materials can reduce the overall cost of structures. The Electromagnetism-like Firefly Algorithm (EFA) was developed by te al. [1] and applied for discrete structural optimization. The improved performance of the EFA in comparison with other optimizers was demonstrated by six optimization problems related to truss structures. An adaptive tist differential evolution (aeDE) was used by Ho-Huu et al. [2] for the optimization of truss structure 6 vith discrete design variables. That technique helps preserve the balance between global and local searching abilities in the differential evolution (DE). Numerical results reveal that aeDE was more efficient than the DE and other methods in terms of the quality of solution and convergence rate.

Metaheuristics such as evolutionary algorithms and swarm intelligence paradigms have been designed for tackling many poblems in various fields as competitive alternative solvers because they do not require gradient information, easy implementation process, and bypass the local optima problem [22-28]. Swarm-based algorithms try to mimic the social behavior of nature creatures who swarm, herds, schools or flocks for foraging, migration and enemy skipping. The swarm-based algorithms comprised of environment and agents. These agents interact with each other in the environment and converge to a common solution for a problem using an environmental mechanism, interaction mechanism, and activities of agents. 5 terms of recently proposed swarm intelligence paradigms, the Coyote Optimization Algorithm (COA) [29] is a promising and competitive stochastic population-based approach for global optimization tasks. It considers the principles of coyote social relations. The Cultural Coyote Optimization Algor 10n (CCOA) was proposed and validated by Pierezan et al. [30] under a set of benchmark functions from the Institute of Electrical and Electronics Engineers (IEEE) Congress on Evolutionary Computation (CEC) 2017 and gas turbine problem. The results showed that the CCOA outperforms stateof-the-art metaheuristics.

Maintaining a good balance between the convergence and the diversity is particularly crucial for the performance of a metaheuristic algorithm. In this context, the key capabilities of metaheuristic algorithms such as COA to be able to find reasonable solutions are exploration and exploitation.

Exploration and exploitation are fundamental concepts of any search algorithm. The exploration are fundamental concepts of any search algorithm. The exploration are different promising regions in a given search space whereas exploitation ensures the searching of optimal solutions around the promising regions, a kind of local search. It is important for a metaheuristic algorithm maintaining an appropriate balance between the exploration and exploitation behaviors be competitive in terms of robustness and performance. However, it is difficult to balance between these phases due to its stochastic nature. A latent viewpoint interprets exploration and exploitation as a global search and local search, respectively. Pure exploration degrades the precision of the search process but increases its capacity to find new potential solutions. On the other hand, pure exploitation allows refining existent solutions but a 15 resly driving the process to locally optimal solutions.

On the other hand, in recent years, growing interests in chaos theory and its features have stimulated 15 e studies of chaos applied in optimization algorithms design. Chaos is a kind of a feature of a nonlinear dynamic system which exhibits bounded unstable dynamic behavior, ergodic, non-period behavior depended on initial condition and control parameters. Due to the benefit of a few properties as stochasticity and ergodicity of chaos, the idea of using chaotic sequences instead of random sequences has been noticed in several fields, one of these fields is the optimization theory [31-40]. In this paper, a modified COA (MCOA) approach based on chaotic sequences generated by Tinkerbell map [41-43] is proposed to improve the exploration behavior. Additionally, an adaptive procedure of updating parameters related to social condition is adopted to update the exploitation behavior based on the historical record f success in the search. The proposed MCOA is validated by truss optimization problems with discrete design variables and focus in minimization of the structure weight under the required

The rest of this paper is organized as follows. Section 2 presents a description of the classical COA and the proposed COA variant using Tinkerbell chaotic map. After, details of the truss optimization problems are shown in Section 3. Finishing, the numerical results and conclusive remarks are given in Sections 4 and 5, respectively.

2. Description of the optimization methods

In this section, the fundamentals of the COA are presented. After, the proposed modified COA using Tinkerbell chaotic map is detailed.

2.1. Coyote optimization algorithm (COA)

Unlike most widespread algorithms, the population in the COA is subdivided in packs and the internal social influences are designed [29]. The COA requires only a few control hyperparameters including the number of packs, the population size, and the number maximum of generations (the stopping criterion). The source code of the COA for single-objective optimization in MATLAB©, R and Python are given in https://github.com/jkpir/

Step 1: 11 otes population initialization. The population (X) is composed of N_p packs with N_c coyotes each and the initialization (iteration t = 0) inside the search space defined by the interval $[lb, ub]^D$ occurs as follows:

$$soc_{c,i}^{p,t} = lb_j + r_j \cdot (ub_j - lb_j), \tag{1}$$

where $c = [1, 2, \dots, N_c]$, $p = [1, 2, \dots, N_p]$, $j = [1, 2, \dots, N_p]$, D, D is the dimension of the optimization problem and r_j is a random number inside [0, 1] generated by a uniform probability distribution. The packs are randomly grouped by the same distribution and the initial coyotes ages $(age_p^{p,0})$ are all equal to 0.

Step 2: Coyote's adaptation. The coyote adaptation is evaluated due to the objective function. It is a consequence of its social condition, which means:

$$fit_c^{p,t} = f(soc_c^{p,t}). (2)$$

While the stopping criterion is not reached, repeat Steps 3 to 10

For each p^{th} pack, repeat Steps 3 to 8.

Step 3: Alpha coyote definition. In nature, the alpha coyote is the one that presents the best social condition. In the COA, it means the best (i.e. the smallest or the highest) objective function cost, or:

$$alpha^{p,t} = \left\{ soc_c^{p,t} | arg_{c=\{1,2,\cdots,N_c\}} min_{f\left(soc_c^{p,t}\right)} \right\}. \tag{3}$$

Step 4 11 he social tendency. The social behavior of coyotes is naturally influenced by the alpha and the other coyotes of the pack. In COA, this phenomenon is represented by the cultural tendency of the pack $(ct^{p,t})$, which is the median of the coyote's social conditions:

$$ct_{j}^{p,t} = median\left(soc_{c,j}^{p,t}\right) \forall c \in \{1, 2, \cdots, N_{c}\}$$

$$\tag{4}$$

for $j = [1, 2, \dots, D]$.

For each c^{th} coyote of the p^{th} pack, repeat Steps 5 to 7.

Step 5: Social condition update. The social condition is updated according to the influence of the alpha coyote (δ_a) and the social tendency (δ_t) , generated from two random coyotes of the pack (cr_1) and cr_2 , which means:

$$new_soc_c^{p,t} = soc_c^{p,t} + r_1 \cdot \delta_t + r_2 \cdot \delta_a$$
 (5)

where

$$\delta_t = \mathsf{ct}^{p,t} - \mathsf{soc}_{ct}^{p,t} \tag{6}$$

$$\delta_a = \mathsf{alpha}^{p,t} - \mathsf{soc}^{p,t} \tag{7}$$

and r_1 and r_2 are, respectively, the weights of the pack and the alpha influence, both random numbers inside the range [0,1] generated with uniform distribution of probability.

Step 6: New social condition evaluation. The objective function cost is calculated considering the new social condition.

$$new_{f}t_{c}^{p,t} = f(new_{s}oc_{c}^{p,t}), \tag{8}$$

Step 7: Adaptation. The coyotes choose the social condition that best fits the environment to keep it to the next iteration, which means the best (i.e. the smallest or the highest) objective function cost, such that:

$$soc_{c}^{p,t+1} = \begin{cases} new_soc_{c}^{p,t}, & \text{if } new_fit < fit_{c}^{p,t} \\ soc_{c}^{p,t}, & \text{otherwise} \end{cases}$$
 (9)

Step 8: Birth and death. Firs 11 pup is generated with age equals to 0 and considering the scatter probability (P_s) and the association probability (P_a), such that:

$$pup_{j}^{p,t} = \begin{cases} soc_{k_{1}j}^{p,t}, & \text{if } rnd_{j} < P_{a} \text{ or } j = j_{1} \\ soc_{k_{2}j}^{p,t}, & \text{if } rnd_{j} \geq P_{s} + P_{a} \text{ or } j = j_{2} \\ R_{j}, & \text{otherwise} \end{cases}$$
(10)

where these probabilities are calculated as follows:

$$P_{s} = \frac{1}{D},\tag{11}$$

$$P_a = \frac{(1 - P_s)}{2_{10}},\tag{12}$$

 k_1 and k_2 are the two selected coyotes from 11 p^{th} pack, j_1 and j_2 are two random dimensions of the problem, k_j is a random number inside the decision variable bound of the j^{th} dimension and rnd_j is a random number inside [0,1] generated with uniform probability distribution. After that, the pup social condition is evaluated and the death rule is applied, according to the following algorithm:

Step Description



- 1 Compute the group of worst adapted coyotes than the pup (ω)
- **2** Compute the number of coyotes inside ω (φ) **If** φ = 1
- 3 The pup survives and the only coyote in ω dies Else if $\omega > 1$
- **4** The pup survives and the oldest coyote in ω dies **Else**
- 5 The pup dies.

Step 9: Transition between packs. Along with the coyote's life, it can evict from a pack and go to another one. In COA, two random coyotes from different packs change their positions with probability P_e , such that:

$$P_e = 0.005 \cdot N_c^2 \tag{13}$$

Step 10: Ages update. The coyotes age is updated every iteration, which means:

$$age_c^{p,t+1} = age_c^{p,t} + 1$$
 (14)

Step 11: Solution selection. The best-adapted coyote among all packs is selected as the solution of the optimization problem.

2.2. Modified coyote optimization algorithm (MCOA)

An important issue that needs to be addressed is [3] value of control parameters of COA (see details in [29,30,44]). The control parameters manage the balance between exploitation (using the existing material in the population to best effect) and exploration

(searching for better coyotes). The control poameters related to the scatter and association probabilities are key factors affecting the COA's convergence.

Choosing suitable control parameter values in COA as in another evolutionary and swarm-based approaches is frequently a problem-dependent task. Suitable control parameters are different for different function problems in giding structural optimization (see examples in [1–21,45]). The difficulty in the use of COA arises in that the choice of these is mainly based on empirical evidence and practical experience.

As mentioned in the Introduction section, the deg n of optimization techniques using chaotic sequences [31–40] has received a great deal of attention in the literature. Optimization approaches using chaotic sequences are generally based on ergodicity, stochastic properties and irregularity of chaotic signals. The use of chaotic

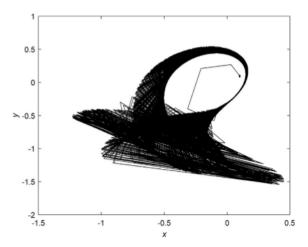


Fig. 1. Phase plots of Tinkerbell map using 3000 iterations.

sequences in COA can be helpful to escape more easily from local minima than can be done through the traditional COA.

In the MCOA, Tinkerbell chaotic mag generating values are adopted. The Tinker lamp [41–43] is an example of a strange attractor, where the two-dimensional quadratic map of its map is given by

$$x_{t+1} = x_t^2 - y_t^2 + a \cdot x_t + b \cdot y_t \tag{15}$$

$$\mathbf{y}_{t+1} = 2\mathbf{x}_t \mathbf{y}_t + \mathbf{c} \cdot \mathbf{x}_t + \mathbf{d} \cdot \mathbf{y}_t \tag{16}$$

where a, b, c, d are non-zero parameters and t is the iteration. For parameter 3 ues (adopted to the COA design with different initial conditions) a = 0.9, b = -0.6013, c = 2.0, and d = 0.5, we get the chaotic attractor of this map as shown in Fig. 1. For generating the Fig. 1, the 3 litial conditions are $x_0 = 0.1$ and $y_0 = 0.1$.

Considering a population with N_p packs with N_c coyotes each, a summary of the MCOA steps is shown in Fig. 2. In step 11, it is adopted a normalized Tinkerbell chaotic map-generating values in 3 range [0, 1] to scatter and association probabilities tuning.

In this case, in a preprocessing phase of Tinkerbell map data to utilization in MCOA, T values are generated using the equations (15) and (16). After the values of x_{t+1} (equation (17)) are normalized using a linear scalar function to scatter and association probabilities tuning. The linear scaling function makes use of the maximum and minimum values of x_{t+1} . The linear scaling function in the range [0.025, 0.075] transforms a variable x_{t+1} into x_{t+1}^* in the following way:

$$x_{t+1}^* = \frac{x_{t+1} - \min(x)}{\max(x) - \min(x)}$$
(17)

where $\mathbf{x} = (x_1, ..., x_T)$, T is number of iterations, $\min(x)$ and $\max(x)$ are the minimum and maximum value 10 f x_{t+1} , respectively.

In the original COA, r_1 and r_2 are random numbers inside the range [0,1] generated with uniform distribution of probability. In terms of exploitation behavior, an adaptive procedure of updating parameters r_1 and r_2 in equation (5) related to social condition is employed in the MCOA based on adaptive differential evolution called JADE. Details about the JADE can be found in [46].

Step	Description
1	Define the control parameters
2	Initialize N_p packs with N_c coyotes each
3	Evaluate the coyote's adaptation
	While stopping criterion is not achieved do
	For each p pack do
4	Define the alpha coyote of the pack
5	Compute the pack's social tendency
	For each c coyote do
6	Update the coyote's social condition
7	Evaluate the new social condition
8	Coyote's adaptation (objective function calculus)
	End for
9	Birth and death inside the pack
	End for
10	Select the population to the next iteration
11	Packs reorganization according to the scatter and association
	probabilities using Tinkerbell chaotic maps
12	Update parameters related to social condition in an adaptive form
13	Update the coyotes' ages
	End while
14	Return the best solution

Fig. 2. Steps of the MCOA.

The adopted procedure in MCOA uses optional external archive and an adaptive parameter method. The external archive not only can provide the progress direction but also can improve the diversity of the swarm. The adaptive parameter method lets the r_1 and r_2 be generated following Gaussian distributions truncated to [0,1]. Their expected mean values are adaptively updated using the successful values of r_1 and r_2 . In general terms, the parameters r_1 and r_2 for each coyote are updated based on their historical record of success.

At each iteration, a r_1 and r_2 are generated for each coyote according to Gaussian distributions with location parameter μ_{r_1} and μ_{r_2} with a standard deviation of 0.1. The parameters μ_{r_1} and μ_{r_2} are initialized to 0.5 and then updated at the end of each generation according to the following equations:

$$\mu_{r1} = (1 - c_r) * \mu_{r1} + c_r * mean_A(S_{r1})$$
(18)

$$\mu_{r2} = (1 - c_r) * \mu_{r2} + c_r * mean_A(S_{r2})$$
 (19)

where c_r is a constant $\in [0, 1]$. S_{r1} and S_{r2} are the set of all successful r_1 and r_2 in the current iteration, and $mean_A(.)$ is the arithmetic mean. In this paper, the adopted c_r equals to 0.05.

3. Benchmarks of truss optimization

In this section, four benchmarks of truss optimization problems including planar 52-bar truss, 72-bar space truss structure, 120-bar dome truss, and planar 200-bar truss structure are described. All adopted benchmarks are constrained optimization problems.

When the problems contain constraints, the feasible region is reduced, leading to many difficulties in solving them. As a rule, in constraint handling methods based on penalty functions [47,48], a penalty term is added to the objective function penalizing the function values outside the feasible region.

In this paper, the county aint-handling strategy utilized by COA and MCOA approaches relies on a simple transformation of the original cost function of the optimization problem. Transforming constrained optimization problem into an unconstrained problem is the core idea of the penalty function whose formula is given by:

$$\varphi(X) = f(X) + p(X) \tag{20}$$

$$p(X) = \gamma * nvc \sum_{i=1}^{m} max(0, g_i(X))^2$$
 (21)

where max is the maximum value, $i=1,\ldots,m$ inequality constraints, f(X) is the objective function (minimization of the structure weight), $\varphi(X)$ is the extended objective function, p(X) is the penalty value defined by the inequality constraints $g_i(X)$, nvc is the number of violated constraints, and γ is a positive constant called penalty factor. The penalty value is added to the fitness function because low values are preferred as expected in a minimization problem. In this paper, γ equals to 10^{20} was adopted.

3.1. A planar 52-bar truss structure

This section carries out the optimization p_1 blem for a 52-bar planar truss structure shown in Fig. 3. The mass density E and the modulus of elasticity q of the constitutive material are respectively 207 GPa and 7860 kg/m³. The tension and compression stress are subjected not to higher than a magnitude of 180 MPa. In this problem, the horizontal and vertical loads that are applied to the nodes from 17 to 20 are set to $P_x = 100$ kN and $P_y = 200$ kN, correspondingly. All bar $P_y = 100$ kN and $P_y = 100$ kN, correspondingly. All bar $P_y = 100$ kN, $P_y = 1$

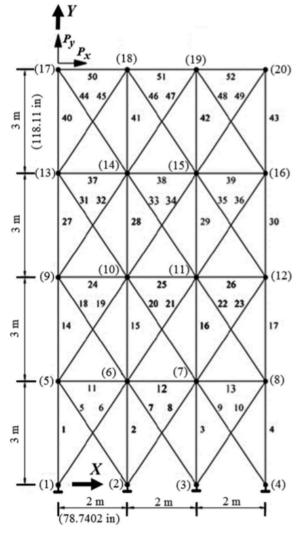


Fig. 3. A 52-bar space truss structure. Source: [15].

each group contains the bars having a same value of the cross-sectional area. Therefore, there are 12 design variables in this optimal design problem. Discrete values of cross-sectional areas can be selected from Table 1.

This problem has been investigated using several optimizate 13 algorithms such as genetic algorithm (GA) and modified GA by Wu and Chow 15, HS by Lee et al. [49], heuristic particle swarm optimization (HPSO) by Li et al. [11], MBA, WCA and IMBA by Sadollah et al. [15,50], colliding bodies optimization (CBO) by Kaveh and Mahd 151, TLBO by Dede [52], hybrid harmony search algorithm (HHS) by Cheng et al. [53], DE and aeDE by Ho-Huu et al. [2].

3.2. A spatial 72-bar space truss structure

The second example executes the optimization problem for a 72-bar space truss structure as shown in Fig. 4. The material density is 0.1 lb/in^3 and the modulus of elasticity is 10^4 ksi . The stress limitations of the members are $\pm 25,000 \text{ psi}$. All nodal displacements must be smaller than $\pm 0.25 \text{ in}$. There are 72 truss elements

Table 1List of the cross-sectional areas from the AISC (American Institute of Steel Construction) design code.

Number	in ²	mm^2	Number	in ²	mm ²
1	0.111	71.613	33	3.840	2477.414
2	0.141	90.968	34	3.870	2496.769
3	0.196	126.451	35	3.880	2503.221
4	0.250	161.290	36	4.180	2696.769
5	0.307	198.064	37	4.220	2722.575
6	0.391	252.258	38	4.490	2896.768
7	0.442	285.161	39	4.590	2961.284
8	0.563	363.225	40	4.800	3096.768
9	0.602	388.386	41	4.970	3206.445
10	0.766	494.193	42	5.120	3303.219
11	0.785	506.451	43	5.740	3703.218
12	0.994	641.289	44	7.220	4658.055
13	1.000	645.160	45	7.970	5141.925
14	1.228	792.256	46	8.530	5503.215
15	1.266	816.773	47	9.300	5999.988
16	1.457	939.998	48	10.850	6999.986
17	1.563	1008.385	49	11.500	7419.340
18	1.620	1045.159	50	13.500	8709.660
19	1.800	1161,288	51	13.900	8967.724
20	1.990	1283.868	52	14.200	9161.272
21	2.130	1374.191	53	15.500	9999.980
22	2.380	1535.481	54	16.000	10,322.560
23	2.620	1690.319	55	16.900	10,903.204
24	2.630	1696.771	56	18.800	12,129.008
25	2.880	1858.061	57	19.900	12,823.684
26	2.930	1890.319	58	22.000	14,193.520
27	3.090	1993.544	59	22.900	14,774.164
28	3.130	2019.351	60	24.500	15,806.420
29	3.380	2180.641	61	26.500	17,096.740
30	3.470	2238.705	62	28.000	18,064.480
31	3.550	2290.318	63	30.000	19,354.800
32	3.630	2341.931	64	33.500	21,612.860

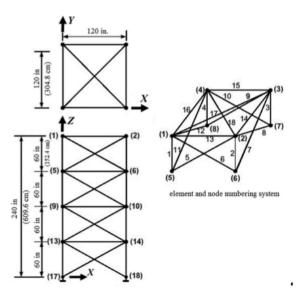


Fig. 4. A 72-bar space truss structure. Source: [56].

6 which are divided into 16 groups: (1) A_1-A_4 , (2) A_5-A_{12} , (3) $A_{13}-A_{16}$, (4) $A_{17}-A_{18}$, (5) $A_{19}-A_{22}$, (6) $A_{23}-A_{30}$, (7) $A_{31}-A_{34}$, (8) $A_{35}-A_{36}$, (9) $A_{37}-A_{40}$, (10) $A_{41}-A_{48}$, (11) $A_{49}-A_{52}$, (12) A_{53} A_{54} , (13) $A_{55}-A_{58}$, (14) $A_{59}-A_{66}$, (15) $A_{67}-A_{70}$, and (16) $A_{71}-A_{72}$. This problem 13 spreviously examined by Li et al. [11], Sadollah et al. [15,50], Wu and Chow [45], Lee et al. [49], Kaveh and Mahdavi [51], Kaveh and Talatahari [54], and Kaveh and Ghazaan [55].

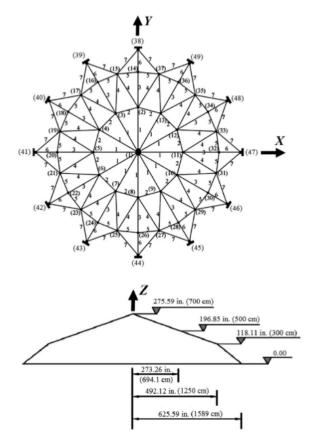


Fig. 5. A 120-bar dome structure. Source: [50].

3.3. A 120-bar dome structure

A 120-bar dome truss, shown in Fig. 5, is considered the third case study. The problem has been studied as a benchmark optimization problem with static constraints. The symmetry of the structure about the X-axis and Y-axis is considered to 120 members into seven independent size variables. A constant lumped mass is attached as 3000 kg (6613,868 lb) at node 1, 500 kg (1102.31 lb) at nodes 2 to 13, and 100 kg (220.462 lb) at the rest of the free nodes. The elements are clustered into 7 groups by considering symmetry about the Z-axis.

This problem was previously solved by Kaveh and Mahdavi [51] using CBO, Kaveh and Zolghadr [58] using democratic particle swarm optimization (DPSO), Kaveh and Zolghadr [59] based on hybridization of the Charged System Search and the Big Bang-Big Crunch algorithms (CSS-BBBC), and Tejani et al. [60] using adaptive symbiotic organisms search (SOS), among others.

3.4. A planar 200-bar truss structure

The fourth case study con Alered for size optimization is the 200-bar plane truss structure. A constant lumped mass of 100 kg is attached at each of the upper nodes (nodes 1–5), whereas all elements are grouped into 29 groups corresponding to 29 design variables by considering geometrical symmetry, as shown in Fig. 6 and Table 2. All member are made of steel: the material density and modulus of elasticity are 0.283 lb/in³ (7933.410 kg/m³) and 30,000 ksi (206,000 MPa), respectively. This truss is subjected to

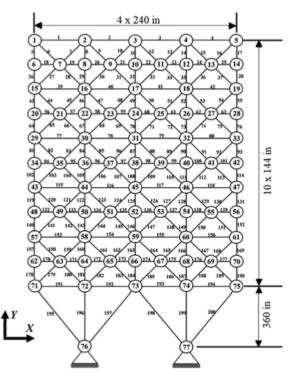


Fig. 6. A 120-bar dome structure. Source: [61].

constraints only on stress limitations of \pm 10 ksi. There are three loading conditions: (i) 1.0 kip acting in the positive *X*-direction at nodes 1, 6, 15, 20, 29, 43, 48, 57, 62, and 71; (ii) 10 kips acting in the negative *Y*-direction at nodes 1, 2, 3, 4, 5, 6, 8, 10, 12, 14, 15, 16, 17, 18, 19, 20, 22, 24, ..., 71, 72, 73, 74, and 75; and (iii) conditions (i) and (ii) acting together. the minimum cross-sectional area of all is 0.1 in² (0.6452 cm²) and the maximum cross-sectional area is 20 in² (129.03 cm²).

This problem was previously solved by Kaveh and Talatahari [61] using a hybrid scheme based on particle swarm optimization, ant colony and harmony search (HPSACO), Lamberti [62] using a simulated annealing approach (SA), Degertekin et al. [63] using a

harmony search approach (SAHS) and Degertekin and Hayalioglu [12] proposed a TLBQ₁₆ ethod. Furthermore, recently Kim and Byun [64] presented a diversity-enhanced cyclic neighborhood network topology particle swarm optimizer (CNNT-PSO).

4. Numerical results

In \bigcap s section, four benchmarks of structure optimization problems with discrete design variables are solved by the COA and MCOA which were described in Section 2. The MCOA was implemented in MATLAB©, adopting the parameters: number of independent runs is 50 times to provide statistically meaningful results, N_p equal to 10 packs, N_c set to 5 coyotes, and stopping criterion of 8000 objective function evaluations, except to the planar 200-bar truss structure with 30,000 objective function evaluations. It is important to mention that the candidate solutions are rounded for the nearest integer (discrete variables) to objective function evaluation.

In this paper, the structural optimization problem minimizes the truss weight by finding the optimal nodal positions and optimal elemental cross-sectional areas such that it satisfies multiple natural frequency constraints. Therefore, the objective function is formulated for the structural weight by neglecting the weight of lumped masses, where nodal coordinates and the element cross-sectional areas are the design variables.

Simulation results in Tables 3–6 show that the MCOA obtained competitive results to planar 52-bar truss (D = 12), spatial 72-bar truss (D = 16), 120-bar dome truss (D = 7) and planar 200 bartruss (D = 29) optimization problems, respectively. The best results in Tables 3–6 are in bold.

In terms of the MCOA for the planar 52-truss case study reported in Table 3, MCOA found an optimum weight of 1902.605 lb after 5392 structural analyses. It suitably agrees with the results obtained by other researches. It outperforms the best result presented in [11] in terms of the best (minimum) of the weights. Furthermore, MCOA presents the same best results than the results mentioned in [1,2,50], but it presents superior results in terms of the mean and worst weight than the results in [1,2,11,50]. However, the IMBA [15] presented superior results considering the mean weight when compared with MCOA.

For the spatial 72-truss case study, the best results in Table 4 for the weights of MCOA outperform the best results presented in [1,2,50,51,54] in terms of the mean of the weights. MCOA achieved

Table 2Design variables for the planar 200-bar truss structure.

Element number (design variable)	Member in the group	Element number (design variable)	Member in the group
1	1, 2, 3, 4	16	82, 83, 85, 86, 88, 89, 91, 92, 103, 104, 106, 107 109, 110, 112, 113
2	5, 8, 11, 14, 17	17	115, 116, 117, 118
3	19, 20, 21, 22, 23, 24	18	119, 122, 125, 128, 131
4	18, 25, 56, 63, 94, 101, 132, 139, 170, 177	19	133, 134, 135, 136, 137, 138
5	26, 29, 32, 35, 38	20	140, 143, 146, 149, 152
6	6, 7, 9, 10, 12, 13, 15, 16, 27, 28, 30, 31, 33, 34, 36, 37	21	120, 121, 123, 124, 126, 127, 129, 130, 141, 142 144, 145, 147, 148, 150, 151
7	39, 40, 41, 42	22	153, 154, 155, 156
8	43, 46, 49, 52, 55	23	157, 160, 163, 166, 169
9	57, 58, 59, 60, 61, 62	24	171, 172, 173, 174, 175, 176
10	64, 67, 70, 73, 76	25	178, 181, 184, 187, 190
11	44, 45, 47, 48, 50, 51, 53, 54, 65, 66, 68, 69, 71, 72, 74, 75	26	158, 159, 161, 162, 164, 165, 167, 168, 179, 186 182, 183, 185, 186, 188, 189
12	77, 78, 79, 80	27	191, 192, 193, 194
13	81, 84, 87, 90, 93	28	195, 197, 198, 200
14	95, 96, 97, 98, 99, 100	29	196, 199
15	102, 105, 108, 111, 114		

Table 3
Optimization results for the planar 52-bar dome structure case study.

Design variable	Le et al. [1] EFA	Ho-Huu et al. [2] aeDE	Li et al. [11] PSO	Sadollah et al. [50] Mine	Sadollah <mark>et al</mark> . [15] WCA	Sadollah et al. [15] IMBA	COA	MCOA
A ₁ -A ₄	4658.055	4658.055	4658.055	4658.055	4658.055	4658.055	4658.055	4658.055
A ₅ -A ₁₀	1161.288	1161.288	1161.288	1161.288	1161.288	1161.288	1161.288	1161.28
A ₁₁ -A ₁₃	494.193	494.193	363,225	494.193	494.193	494.193	494.193	494.193
A ₁₄ -A ₁₇	3303.219	3303.219	3303.219	3303,219	3303.219	3303,219	3303.219	3303.219
A ₁₈ -A ₂₃	939.998	939.998	940.000	939.998	940.000	940.000	939.998	939.998
A ₂₄ =A ₂₆	494.193	494.193	494.193	494.193	494.193	494.193	494.193	494.193
A ₂₇ -A ₃₀	2238.705	2238.705	2238.705	2238.705	2283.705	2283.705	2238.705	2238.70
A ₃₁ -A ₃₆	1008.385	1008.385	1008.385	1008.385	1008.385	1008.385	1008.385	1008.38
A ₃₇ -A ₃₉	494.193	494.193	388.386	494.193	494.193	494.193	494.193	494.193
A ₄₀ -A ₄₃	1283.868	1283.868	1283.868	1283.868	1283.868	1283.868	1283.868	1283.86
A ₄₄ -A ₄₉	1161.288	1161.288	1161.228	1161,288	1161.288	1161.288	1161.288	1161.28
A ₅₀ =A ₅₂ 14	494.193	494.193	792,256	494.193	494.193	494.193	494.193	494.193
Best weight (Ib)	1902.605	1902.605	1905.490	1902,605	1902.605	1902.605	1902.605	1902.60
Worst weight (lb)	1910.942	1925.714	-	1912.646	1912.646	1904.830	1931.551	1908.92
Mean weight (lb)	1904.775	1906.735	-	1906.076	1909.856	1903.076	1909.172	1903.92
Standard deviation (lb)	3.045	6.679	-	4.090	7.090	1.130	8.129	2.913
Number of structural analysis	2894	3402	-	5450	7100	4750	7050	5390

Table 4Optimization results for the spatial 72-bar truss case study.

Design variable	Le et al. [1] EFA	Ho-Huu et al. [2] aeDE	Kaveh and Talatahari [54]DHPSACO	Sadollah et al. [50] Mine	Sadollah et al. [15] WCA	Sadollah et al. [15] IMBA	Kaveh and Mahdavi [51] CBO	COA	MCOA
A ₁ -A ₄	1.990	1.990	1.800	0.196	1.990	1.990	1.620	1.990	1.990
A ₅ -A ₁₂	0.563	0.563	0.442	0.563	0.442	0.442	0.563	0.563	0.563
A ₁₃ -A ₁₆	0.111	0.111	0.141	0.442	0.111	0.111	0.111	0.111	0.111
A ₁₇ -A ₁₈	0.111	0.111	0.111	0.602	0.111	0.111	0.111	0.111	0.111
A ₁₉ =A ₂₂	1.228	1.228	1.228	0.442	1.266	1.266	1.457	1.228	1.228
A ₂₃ -A ₃₀	0.442	0.442	0.563	0.442	0.563	0.563	0.442	0.442	0.442
A ₃₁ -A ₃₄	0.111	0.111	0.111	0.111	0.111	0.111	0.111	0.111	0.111
A ₃₅ -A ₃₆	0.111	0.111	0.111	0.111	0.111	0.111	0.111	0.111	0.111
A ₃₇ -A ₄₀	0.563	0.563	0.563	1.266	0.422	0.422	0.602	0.563	0.563
A ₄₁ -A ₄₈	0.563	0.563	0.563	0.563	0.422	0.422	0.563	0.563	0.563
A ₄₉ =A ₅₂	0.111	0.111	0.111	0.111	0.111	0.111	0.111	0.111	0.111
A ₅₃ -A ₅₄	0.111	0.111	0.250	0.111	0.111	0.111	0.111	0.111	0.111
A ₅₅ -A ₅₈	0.196	0.196	0.196	1.800	0.196	0.196	0.196	0.196	0.196
A ₅₉ -A ₆₆	0.563	0.563	0.563	0.602	0.563	0.563	0.602	0.563	0.563
A ₆₇ -A ₇₀	0.391	0.391	0.442	0.111	0.442	0.442	0.391	0.391	0.391
A ₇₁ =A ₇₂	0.563	0.563	0.563	0.111	0.602	0.602	0.563	0.563	0.563
Material Meight (lb)	389.334	389.334	390.380	390.730	389.334	389.334	391.070	389.334	389.33
Worst weight (lb)	393.325	393.826	-	399.490	393.778	389.457	495.970	393.965	392.15
Mean weight (lb)	390.913	391.376	-	395.432	389.941	389.823	403.710	393.618	390.16
Standard deviation (lb)	1.161	1.376	-	3.040	1.430	0.840	24.800	1.561	1.018
Number of structural analysis	3123	4101	-	11,600	4600	6250	6000	6800	5750

Table 5Optimization results for the spatial 120-bar dome case study.

Design variable	Kaveh and Mahdavi [51] CBO	Kaveh and Zolghadr [58] DPSO	Kaveh and Zolghadr [59] CSS- BBBC	Tejani et al. [60] SOS	COA	MCOA
1	19.6917	19.607	17.448	19.5715	19.4994	19.4994
2	41.1421	4.1290	49.076	39.8327	40.3890	40.3890
3	11.1550	11.136	12.365	10.5879	10.6073	10.6073
4	21.3207	21.025	21.979	21.2194	21,1126	21,1126
5	9.8330	10.060	11.190	10.0571	9.8420	9.8420
6	12.8520	12.758	12.590	11.8322	11.7715	11.7715
7	15.1602	15.414	13.585	14.7503	14.8384	14.8384
Best weight (kg)	8889.1303	8890.48	9046.34	8710.33	8707.2432	8707.2432
Worst weight (kg)	_	_	-		8737.1328	8734.495
Mean weight (kg)	8891.2540	8895.99	-		8720,5461	8713.487
Standard deviation (kg)	1.7926	89.38	-		6.9123	9.1185
Number of structural analysis	6000	6000	4000	4000	5600	5250

Table 6
Optimization results for the planar 200-bar truss structure.

Design variable	Kaveh and Talatahari [54] HPSACO	Lamberti [62] SA	Degertekin [63] SAHS	Degertekin and Hayalioglu [12] TLBO	Kim and Byun [64] CNNT-PSO	COA	MCOA
1	0.1033	0.1468	0.154	0.146	0.1482	0.1441	0.1390
2	0.9184	0.9400	0.941	0.941	0.9405	0.9395	0.9355
3	0.1202	0.1000	0.100	0.100	0.1000	0.1000	0.1000
4	0.1009	0.1000	0.100	0.101	0.1000	0.1000	0.1000
5	1.8664	1.9400	1.942	1.941	1.9408	1.9395	1.9355
6	0.2826	0.2962	0.301	0.296	0.2975	0.2947	0.2909
7	0.1000	0.1000	0.100	0.100	0.1000	0.1000	0.1000
8	2.9683	3.1042	3.108	3.121	3.1067	3.1027	3.0816
9	0.1000	0.1000	0.100	0.100	0.1000	0.1000	0.1000
10	3.9456	4.1042	4.106	4.173	4.1067	4.1027	4.0816
11	0.3742	0.4034	0.409	0.401	0.4057	0.3987	0.3967
12	0.4501	0.1912	0.191	0.181	0.1897	0.1831	0.2959
13	4.96029	5.4284	5.428	5.423	5.4343	5.3821	5.3854
14	1.0738	0.1000	0.100	0.100	0.1000	0.1000	0.1000
15	5.9785	6.4284	6.427	6.422	6.4340	6.3821	6.3853
16	0.78629	0.5734	0.581	0.571	0.5745	0.5720	0.6332
17	0.73743	0.1327	0.151	0.156	0.1366	0.3389	0.1842
18	7.3809	7.9717	7.973	7.958	7.9803	7.9871	8.0396
19	0.66740	0.1000	0.100	0.100	0.1000	0.1000	0.1000
20	8.3000	8.9717	8.974	8.958	8.9802	8.9871	9.0395
21	1.19672	0.7049	0.719	0.720	0.71089	0.8188	0.7460
22	1.0000	0.4196	0.422	0.478	0.4659	0.1435	0.1306
23	10.8262	10.8636	10.892	10.897	10.9110	10.9723	10.9114
24	0.1000	0.1000	0.100	0.100	0.1000	0.1000	0.1000
25	11.6976	11.8606	11.887	11.897	11.9112	11.9722	11.9114
26	1.3880	1.0339	1.040	1.080	1.0712	0.8947	0.8627
27	4.9523	6.6818	6.646	6.462	6.5030	6.7474	6.9169
28	8.8000	10.8113	10.804	10.799	10.7210	10.8536	10.9674
29 14	14.6645	13.8404	13.870	13.922	13.9310	13.7759	13.6742
Best weight (lb)	25,156.5	25,445.63	25,491.9	25,488.15	25,453.0957	25,453.11	25,450.1
Worst weight (lb)	_	_	25,799.3	25,563.05	25,466.0958	25,666.43	25,557.5
Mean weight (lb)	-	-	25,610.2	25,533.14	25,459.1089	25,545.51	25,522.0
Standard deviation (lb)	-	-	141.85	27.44	3.1544	52.74	47.62
Number of structural analysis			19,670	28,059	1,500,000	29,750	27,720

the best weight as 389.334 lb after a minimum of 5750 structural analyses. In this case, the IMBA [15] found the best results in terms of the mean weight of all tested optimizers.

Table 5 provides the design variables and compares the results obtained by using the COA and MCOA and those of other researches for the spatial 120-bar dome case study. It can be observed that the MCOA was the most efficient optimizer in terms of optimized weight and robustness when compared with the proposed approaches in [51,58–60] in terms of mean and best objection values. All optimization runs of COA and MCOA were successful and converged to a feasible design.

According to Table 6, the result obtained by the MCOA is meaningfully lighter than those of the SAHS [63] and TLBO [12] approaches. It can be observed that MCOA is competitive with the other optimizers such as [12,62,63] in finding optimum designs considered in this study. Furthermore, the mean weight is close to the best weight and a small standard deviation on optimized weight is observed. The results of the COA and MCOA satisfied all design constraints with feasible solutions. The COA and MCOA obtained results without violation of the constraints. Kim and Byun [64] commented on the feasibility of the solutions presented in the literature for the planar 200-bar truss structure.

5. Concluding remarks and direction of future research

In this paper, a modified version of the Coyote Optimization Algorithm (COA) denoted MCOA was proposed to solve four structures optimization problems. This version uses the Tinkerbell chaotic map-generating to define the scatter and association probabilities and an adaptive procedure of updating parameters related to social condition.

The results showed that the MCOA is competitive with recent results from literature in terms of the best and mean (objective function values to 50 runs) measures as presented in Tables 3–6. Comparing the MCOA with the original COA, the worst measures were smaller in both cases, which means that the robustness of the algorithm was improved.

In future works, further improvements on the MCOA using ensemble strategies will be a pursuit to other optimization classes and multiobjective approaches in structural optimization.

8 Declaration of Competing Interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

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