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Makalah

A Modeling of Multi-Echelon Suppliers' Chain for Deteriorating Items

Jonas Yu^{1,2}, G.A. Widyadana³

Abstract: Inventory models for a policy of retail pricing and perishable items have been developed in many papers, but very few of the studies incorporate both of these effects. This study integrates the two conditions from a three-echelon supplier's chain and offers a mathematical modeling for deteriorating inventory system with an optimal joint-cost policy. Exponentially deteriorating items with no shortages is assumed in this study. Two scenarios are considered. Scenario 1 assumed one supplier, one distributor and one retailer occurs at the regular inventory replenishment time, and scenario 2 assumes two suppliers, one distributor and two competitive retailers that to address this issue, we broaden the benchmark setting by letting the independent retailer channel be a duopoly. The mathematical model describes how the integrated approach to decision making can achieve global optimality as compared to independent decision by the suppliers, the distributor, and the retailers. A computer code is developed to derive the optimal solution. Numerical examples and sensitivity analysis are given to validate the results of the system.

Keywords: Deterioration, supply chain, three-echelon inventory system.

Introduction

Historically, the three key members of the supply chain, supplier, distributor and retailer, have been managed independently, buffered by large inventories. Increasing competitive pressures and decreasing marginal profitability are forcing firms to develop supply chains that can quickly respond to customer needs and furthermore reduce the cost on carrying inventory. There are three fundamental stages in the supplier chain: Procurement, production and distribution. Through their coordination, the number of deliveries is derived in corporation with each other to achieve a minimum overall integrated cost.

Deterioration is defined as decay, damage, spoilage, evaporation, obsolescence, pilferage, and loss of utility or loss of marginal value of a commodity that results in decreasing usefulness from the original one. Blood, fish, strawberries, alcohol, gasoline, radioactive chemicals and grain products are examples of deteriorating commodities. In this study, deterioration is assumed to be a function of the on-hand inventory within the whole supplier chain.

In order to reduce loss due to deterioration of the products, the members of the supply chains frequently

implement a joint decision to the optimal number of deliveries.

Ghare and Schrader [3] were the first authors to consider on-going deterioration of inventory. Then, several researchers have studied deteriorating inventory in recent decades. Bessler and Veinott [2] made the analysis on the integration between the buyer and the supplier by developing a mathematical model with an arborescent structure. Axsater [1] have developed the different models based on the centralized and decentralized echelon. Wee [7] derived the integration model between vendor and buyer for deteriorating items. Rau *et al.* [5] developed production inventory model for deteriorating items under multi echelon supply chain. Similar model is introduced by Rau *et al.* [6]. In their model they considered supplier-buyer integrated model by taking account buyer shortage. Later Lin and Lin [4] developed two-echelon inventory model by considering completed backorder in the problem.

In this paper, a mathematical model taking into account the integration of the producer, distributor and retailer is developed. Since the three players do not have production rate constraints, so the model is different with Rau *et al.* [5]. Rau *et al.* [5] considered three players in their model who are supplier, producer and buyer. They assumed that the producer has specific production rate. Yu [8] proposed an integrated deteriorating inventory model for a multi-echelon supply chain with dual source. The numerical example shows that the integrated approach that takes account of the supplier, the distributor and the retailer is better than the independent approach by the individual player. The model has potential application in a supply chain environment where there is a multi-echelon inventory system. This

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three-echelon inventory system usually happens in real life.

Methods

Mathematical Model

The mathematical model is developed on the basis of the following assumptions: (a) the demand rate is known and constant; (b) no shortage is allowed; (c) there is no constraint in space, capacity or capital; (d) the rate of replenishment in either distributor or retailers is infinite and on the same time; (e) a constant fraction the on-hand inventory deteriorates and no replacement of deteriorated items is assumed; (f) only a single-product item is considered.

The following notation is used in this study:

- TC : total joint cost for supply chain
- TC_r : total cost for all retailers
- TC_d : total cost for distributor
- TC_p : total cost for all suppliers
- $Q_{rk}(t)$: retailer's inventory level at any time t , $k = 1,2,3$
- $Q_d(t)$: distributor's inventory level at any time t
- $Q_{pi}(t)$: suppliers's inventory level at any time t , $i = 1, 2$
- C_{rk} : ordering cost for retailers, $k = 1,2,3$
- C_d : ordering cost for distributor
- C_{pi} : ordering cost for suppliers, $i = 1, 2$
- H_{rk} : carrying cost per unit per unit time for retailers, $k = 1,2,3$
- H_d : carrying cost per unit per unit time for distributor
- H_{pi} : carrying cost per unit per unit time for suppliers, $i = 1, 2$
- P_{rk} : deterioration cost per unit per unit time for retailers, $k = 1,2,3$
- P_d : deterioration cost per unit per unit time for distributor
- P_{pi} : deterioration cost per unit per unit time for suppliers, $i = 1, 2$
- d_i : demand rate for retailers , $k = 1,2,3$
- θ : deterioration rate
- m_i : order arrangement rate, $i = 1,2$
- T : replenishment cycle time for suppliers
- t_{ri} : replenishment cycle time for retailers , $i = 1,2,3,\dots,n$
- t_d : replenishment cycle time for distributor
- n_{10} : number of deliveries per cycle time T from suppliers to distributor
- n_{0k} : number of deliveries per cycle time t_d from distributor to retailers, $k = 1,2,3$

As an illustration, the supplier-distributor-retailer inventory system is depicted in Figure 1.

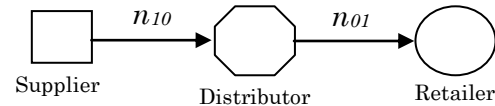


Figure 1. Supplier-distributor-retailer inventory system

We consider the supply chain system consisting of one supplier, one distributor and one retailer, purchasing an item through this chain.

The Retailers' Deteriorating Inventory System

In general, a retailer's deteriorating inventory system is described as follows:

Retail demand depends on two elements—primary demand for the product and store-level factors that influence consumers' sensitivity to retail. Specifically, let p represent price, and retail demand be $q_i = \alpha - \beta p_i$ where $\alpha > 0$ represents the primary demand and $\beta > 0$ represents the store-level factors. The consumers' price decreases proportionally with time going.

$$p_i = p_{i-1}\lambda, 0 < \lambda < 1, i = 1, \dots, n$$

where λ represents the proportional number. The life cycle time of product is t_i . It means the finished goods should be sold out by the time.

The change inventory level, $dQ_{ri}(t)$, during an infinitesimal time, dt , is a function of the deterioration rate, demand rate d and the inventory level $Q_{ri}(t)$. It is formulated as

$$\frac{dQ_{ri}(t)}{dt} = -d - \theta Q_{ri}(t), 0 \leq t \leq t_{ri} \quad (1)$$

For a periodic cycle of t_{ri} , the inventory level $Q_{ri}(t_{ri}) = 0$ and at the initial time, $Q_{ri}(t_{ri}) = S_{ri}$; the solution of (1), after adjusting for the constant of integration is

$$Q_{ri}(t) = \frac{d_i}{\theta} [e^{\theta(t_{ri}-t)} - 1], 0 \leq t \leq t_{ri} \quad (2)$$

From equation (1) and (2), the initial inventory level can be derived as:

$$S_{ri} = \frac{-d_i + d_i e^{\theta t_{ri}}}{\theta} \quad (3)$$

and the deterioration amount during t_{ri} is

$$W_{ri} = S_{ri} - d_i t_{ri} = \frac{-d_i + d_i e^{\theta t_{ri}}}{\theta} - d_i t_{ri} = A_{ri} \theta \quad (4)$$

From equation (4), the carrying inventory during t_{ri} can be derived as:

$$A_{ri} = \frac{d_i e^{\theta t_{ri}} - d_i - \theta d_i t_{ri}}{\theta^2} \quad (5)$$

Therefore, the retailer's carrying cost HC_{ri} for a periodic cycle is given by:

$$HC_{ri} = A_{ri} \times H_r = \left[\frac{d_i e^{\theta t_{ri}} - d_i - \theta d_i t_{ri}}{\theta^2} \right] H_r \quad (6)$$

The retailers inventory cost per replenishment period t_{rk} is depicted by the following formula:
 period cost = ordering cost + carrying cost + deteriorating cost

$$TC_{ri} = q_i c + \frac{d e^{\theta t_{ri}} - d - \theta d t_{ri}}{\theta^2} H_r + \frac{-d + d e^{\theta t_{ri}} - \theta d t_{ri}}{\theta} P_r \quad (7)$$

Thus, we obtain the total cost TC_r through the production cycle is given by:

$$TC_r = \sum_{i=1}^n TC_{ri} \quad (8)$$

$$= \sum_{i=1}^n \left(q_i c + \frac{d e^{\theta t_{ri}} - d - \theta d t_{ri}}{\theta^2} H_r + \frac{-d + d e^{\theta t_{ri}} - \theta d t_{ri}}{\theta} P_r \right)$$

where

$$t_{ri} = \frac{q_{ri}}{d} = \frac{\alpha - \beta p_i}{d} \quad (9)$$

The Distributor's Deteriorating Inventory System

The change inventory level, $dQ_d(t)$, during an infinitesimal time, dt , is a function of the deterioration rate, demand rate d_k and the inventory level $Q_d(t)$. It is formulated as

$$\frac{dQ_d(t)}{dt} = -\sum_{k=1}^3 d_k - \alpha Q_d(t), 0 \leq t \leq t_d \quad (10)$$

For a periodic cycle of t_d , the inventory level $Q_d(t_d) = 0$ and at the initial time, $Q_d(0) = S_d$; the solution of (10), after adjusting for the constant of integration is

$$Q_d(t) = \frac{\sum_{k=1}^3 d_k}{\alpha} [e^{\alpha(t_d-t)} - 1], 0 \leq t \leq t_d \quad (11)$$

From equation (10) and (11), the initial inventory level can be derived as:

$$S_d = \frac{-\sum_{k=1}^3 d_k + \sum_{k=1}^3 d_k e^{\alpha t_d}}{\alpha} \quad (12)$$

and the deterioration amount during t_d is

$$W_d = S_d - \sum_{k=1}^3 d_k t_d - \sum_{k=1}^3 W_{rk} = A_d \alpha \quad (13)$$

Thus, the deterioration cost is

$$W_d \times P_d = \left[\frac{-\sum_{k=1}^3 d_k + \sum_{k=1}^3 d_k e^{\alpha t_d} - \alpha \sum_{k=1}^3 d_k t_d}{\alpha} - \sum_{k=1}^3 \frac{-d_k + d_k e^{\alpha t_{rk}} - \alpha d_k t_{rk}}{\alpha} \right] P_d \quad (14)$$

From equation (13), the carrying inventory during t_d can be derived as:

$$A_d = \left[\frac{-\sum_{k=1}^3 d_k + \sum_{k=1}^3 d_k e^{\alpha t_d} - \alpha \sum_{k=1}^3 d_k t_d}{\alpha^2} - \sum_{k=1}^3 \frac{-d_k + d_k e^{\alpha t_{rk}} - \alpha d_k t_{rk}}{\alpha^2} \right] \quad (15)$$

Thus, the distributor's carrying cost HC_d for a periodic cycle is given by:

$$HC_d = A_d \times H_d \quad (16)$$

Therefore, the total cost for distributor is

$$TC_d(T) = C_d \times n_{10} + HC_d \times n_{10} + W_d \times n_{10}$$

$$= C_d \times n_{10} + \left[\frac{-\sum_{k=1}^3 d_k + \sum_{k=1}^3 d_k e^{\alpha t_d} - \alpha \sum_{k=1}^3 d_k t_d}{\alpha^2} - \sum_{k=1}^3 \frac{-d_k + d_k e^{\alpha t_{rk}} - \alpha d_k t_{rk}}{\alpha^2} \right] H_d \times n_{10} + \left[\frac{-\sum_{k=1}^3 d_k + \sum_{k=1}^3 d_k e^{\alpha t_d} - \alpha \sum_{k=1}^3 d_k t_d}{\alpha} - \sum_{k=1}^3 \frac{-d_k + d_k e^{\alpha t_{rk}} - \alpha d_k t_{rk}}{\alpha} \right] P_d \times n_{10} \quad (17)$$

The Suppliers' Deteriorating Inventory System

The change inventory level, $dQ_{pi}(t)$, during an infinitesimal time, dt , is a function of the deterioration rate α , demand rate d_k , the order arrangement rate m_i and the inventory level $Q_{pi}(t)$. It is formulated as

$$\frac{dQ_{pi}(t)}{dt} = -\sum_{k=1}^3 m_i d_k - \alpha Q_{pi}(t), 0 \leq t \leq T, \text{ where } \sum_{i=1}^2 m_i = 1 \quad (18)$$

For a periodic cycle of T , the inventory level $Q_{pi}(T) = 0$ and at the initial time, $Q_{pi}(0) = S_{pi}$; the solution of (18), after adjusting for the constant of integration is

$$Q_{pi}(t) = \frac{\sum_{k=1}^3 m_i d_k}{\alpha} [e^{\alpha(T-t)} - 1], 0 \leq t \leq T \quad (19)$$

From equation (18) and (19), the initial inventory level can be derived as:

$$S_{pi} = \frac{-\sum_{k=1}^3 d_k m_i + \sum_{k=1}^3 d_k m_i e^{\alpha T}}{\alpha} \quad (20)$$

and the deterioration quantity during T is

$$W_{pi} = S_{pi} - \sum_{k=1}^3 m_i d_k T - m_i W_d$$

$$= \frac{-\sum_{k=1}^3 d_k m_i + \sum_{k=1}^3 d_k m_i e^{\alpha T}}{\alpha} - \sum_{k=1}^3 m_i d_k T - \left(\sum_{k=1}^3 \frac{-d_k + d_k e^{\alpha t_d} - \alpha d_k t_d}{\alpha} - \sum_{k=1}^3 \frac{-d_k + d_k e^{\alpha t_{rk}} - \alpha d_k t_{rk}}{\alpha} \right) m_i$$

$$= A_{pi} \alpha \quad (21)$$

Thus, the deterioration cost is

$$W_{pi} \times P_{pi} = \sum_{k=1}^3 \left[\left(\frac{-d_k m_i + d_k m_i e^{\alpha t_d} - \alpha m_i d_k t_d}{\alpha} \right) - \left(\frac{-d_k + d_k e^{\alpha t_d} - \alpha d_k t_d}{\alpha} - \frac{-d_k + d_k e^{\alpha t_{rk}} - \alpha d_k t_{rk}}{\alpha} \right) m_i \right] \times P_{pi} \tag{22}$$

From equation (21), the carrying inventory within t_d can be derived as:

$$A_{pi} = \sum_{k=1}^3 \left[\left(\frac{-d_k m_i + d_k m_i e^{\alpha t_d} - \alpha m_i d_k t_d}{\alpha^2} \right) - \left(\frac{-d_k + d_k e^{\alpha t_d} - \alpha d_k t_d}{\alpha^2} - \frac{-d_k + d_k e^{\alpha t_{rk}} - \alpha d_k t_{rk}}{\alpha^2} \right) m_i \right] \tag{23}$$

Thus, the supplier's carrying cost HC_{pi} for a periodic cycle is given by:

$$HC_{pi} = A_{pi} \times H_{pi} \tag{24}$$

Thus, the total cost for suppliers is

$$TC_p(T) = \sum_{i=1}^2 (C_{pi} \times n_{10} + HC_{pi} \times n_{10} + W_{pi} \times n_{10}) = \sum_{i=1}^2 C_{pi} \times n_{10} + \sum_{i=1}^2 \sum_{k=1}^3 \left[\left(\frac{-d_k m_i + d_k m_i e^{\alpha t_d} - \alpha m_i d_k t_d}{\alpha^2} \right) - \left(\frac{-d_k + d_k e^{\alpha t_d} - \alpha d_k t_d}{\alpha^2} - \frac{-d_k + d_k e^{\alpha t_{rk}} - \alpha d_k t_{rk}}{\alpha^2} \right) m_i \right] H_{pi} n_{10} + \sum_{i=1}^2 \sum_{k=1}^3 \left[\left(\frac{-d_k m_i + d_k m_i e^{\alpha t_d} - \alpha m_i d_k t_d}{\alpha} \right) - \left(\frac{-d_k + d_k e^{\alpha t_d} - \alpha d_k t_d}{\alpha} - \frac{-d_k + d_k e^{\alpha t_{rk}} - \alpha d_k t_{rk}}{\alpha} \right) m_i \right] P_{pi} n_{10} \tag{25}$$

The Integrated Three-Echelon Deteriorating Inventory System

The integrated total cost can be obtained as:

$$TC = TC_r + TC_d + TC_p \tag{26}$$

The optimal values of $T, n_{10}, n_{01}, n_{02}$ and n_{03} denoted by $T^*, n_{10}^*, n_{01}^*, n_{02}^*$ and n_{03}^* respectively, must satisfy equations (27) and (28), and will be located in the vicinity of $n_{0k}^{\#}$ that satisfy equation (29).

$$\frac{dTC}{dT} = 0 \tag{27}$$

$$TC(n_{ik}^* - 1) \geq TC(n_{ik}^*) \geq TC(n_{ik}^* + 1) \tag{28}$$

$$\frac{dTC}{dn_{ik}^{\#}} = 0 \tag{29}$$

where $i = 0,1$ and $k = 0,1,2,3$

Result and Discussion

Numerical Example

A numerical example is used to illustrate this case discussed. The related data from suppliers are as follows: $T=1$ year, $H_{pi}=H_{p2}=\$5$ per year, $C_{pi}=C_{p2}=\$5000$ per time, $P_{pi}=P_{p2}=\$20$ per unit, $m_i=m_2=0.5$. The related data from distributor are as follows: $H_d=\$20$ per unit per year, $C_d=\$1000$ per time, $P_d=\$30$ per unit. The related data from retailers are as follows: $d_i=d_2=10000, d_3=6000, H_{ri}=H_{r2}=\50 per unit per year, $H_{r3}=\$70$ per unit per

year, $C_{r1}=C_{r2}=\$600$ per time, $C_{r3}=\$600$ per time, $P_{r1}=P_{r2}=\$50$ per unit, $P_{r3}=\$80$ per unit, $\theta=0.05$. The numerical results are tabulated in Table 1. The sensitivity analysis for varying rates of demand, the retailers' carrying cost, the retailers' deterioration cost, the distributor's carrying cost, the suppliers' carrying cost and rates of deterioration are tabulated in Table 2.

Comment on the Sensitivity Analysis

The main conclusions found from the sensitivity analysis are as follows:

- (1) When the retailers' demand rate increases, each player's total cost TC_r, TC_d, TC_p ; the joint total cost TC as well as the number of n_{0k}^* will increase also.
- (2) When the distributor, the suppliers and the retailers' carrying cost increases, the number of n_{10}^* remains the same, but the number of n_{01}^* tends to decrease. If the carrying cost decreases, the reverse is also true.
- (3) As the retailers' deterioration cost increases, the number of deliveries from distributor to retailers tends to increase. Each player's total cost, except the suppliers' cost tends to increase. The joint total cost TC increases as well.
- (4) As soon as the deterioration rate increases, each player's total cost and the joint total cost tend to increase. But, the number of deliveries remains the same.
- (5) The joint total cost TC is more sensitive to the parameter of the distributor's carrying cost H_d . The increase is over 20% as H_d increases by 30%.

Table 1. TC with different combinations of n_{ik}

T	n_{10}	n_{01}	n_{02}	n_{03}	TC_r	TC_d	TC_p	TC^*
1	1	1	1	1	761007	20829	23219**	805056
1	1	5	5	23	125610	277077	23219	425906
1	1	20	20	34	63605	284665	23219	371489
1*	1*	21*	21*	33*	63551*	284708	23219	371478*
1	1	24	24	29	64150	284798	23219	372168
1	2	1	1	1	379432	11832**	665860	1057124
1	2	1	1	22	280949	42021	665860	988830
1	2	24	24	33	85106	142721	665860	893687

Notes: * Optimal solution that minimizes TC .

** Optimal solution that minimizes TC_p or TC_d .

Table 2. Sensitivity analysis when a parameter is changed.

Parameter	% changed	n_{10}^*	n_{01}^*	n_{02}^*	n_{03}^*	TC_r	TC_d	TC_p	$TC(n_{ik}^*)$
	No change	1	21	21	33	63551	284708	23219	371478
d_i	-30%	1	17	21	33	59460	251898	21694	333053
	+30%	1	23	21	33	67088	317484	24745	409317
H_{ri}	-30%	1	23	21	33	59681	284589	23219	367489
	+30%	1	17	21	33	66925	284746	23219	374891
P_{ri}	-30%	1	21	21	33	63389	284685	23220	371293
	+30%	1	20	21	33	63729	284708	23219	371657
H_d	-30%	1	20	21	33	63551	205544	23219	292314
	+30%	1	21	21	33	63603	363811	23219	450633
H_{pi}	-30%	1	21	21	33	63551	284708	23219	371478
	+30%	1	21	21	33	63551	284708	23219	371478
θ	-30%	1	21	21	33	63111	277315	19207	359633
	+30%	1	20	20	33	64024	292125	27272	383422

Conclusion

This paper discusses the optimal joint-cost policy in a two-suppliers three-echelon inventory model that integrates the upper, middle, and lower levels of the supply chain. By using the integrated approach that takes account of the suppliers, the distributor and the retailers, the total joint cost is found to be less than the independent approach by the individual player. The result is validated through sensitivity analysis. Furthermore, recent advances in communications and information technology provide greater opportunity for significant savings in logistics cost by implementing strategic alliances within the supply chains.

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